

Porter Scobey

http://cs.stmarys.ca/~porter/csc/ref/stl/index_algorithms.html

Stanford 106L, Standard C++ Programming Laboratory

<http://web.stanford.edu/class/cs106l/>

topcoder's tutorial, Power up C++ with the STL, part I and II

<https://www.topcoder.com/community/data-science/data-science-tutorials/power-up-c-with-the-standard-template-library-part-1/>

STL Algorithms



`<algorithm>`, `<numeric>`, `<iterator>`, `<functional>`
`<cctype>`, `<cmath>`

C++, a multi-paradigm programming language,
besides being procedural and object-oriented,
is very much *functional* with STL

Pei-yih Ting

NTOU CS

Contents

1. Why STL algorithm?
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Abstract away some chores

data.txt

```
100  
95  
92  
89  
100  
...
```

Average = ...

Abstract away some chores

data.txt

Commonly seen procedural piece of codes

```
#include <iostream>
#include <fstream>
#include <set>
using namespace std;
int main() {
    ifstream input("data.txt");
    multiset<int> values;

    int currValue;
    while (input >> currValue)
        values.insert(currValue);

    double total = 0.;
    for (multiset<int>::iterator itr = values.begin(); itr != values.end(); ++itr)
        total += *itr;

    cout << "Average = " << total / values.size() << endl;
    return 0;
}
```

low-level mechanical steps

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copy(istream_iterator<int>(input), istream_iterator<int>(),
    inserter(values, values.begin()));
```

<algorithm>

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Functional
abstraction

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copy(istream_iterator<int>(input), istream_iterator<int>(),
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```

map

② Add the values together

```
double total = accumulate(values.begin(), values.end(), 0.0);
```

reduce

<numeric>

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cout << "Average = " << total / values.size() << endl;
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- ❖ **Functional and Object-oriented styles are not easy to combine.**
- ❖ Bjarne Stroustrup's: C++ was designed to allow programmers to **switch** between paradigms as needed. The language is not designed to make it easy for combining different paradigms. Most of Stroustrup's examples regarding OOP touch the STL very little. He creates very distinct layers.

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customized with **callable objects**
(functions and functors)

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accumulate()

Your first high-level machinery

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multiset<int> values;
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double total = accumulate(values.begin(), values.end(), 0.0);
accumulate(values.lower_bound(42), values.upperbound(99), 0.0);
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```
int findLess(int smallestSoFar, int current) {
    return current < smallestSoFar ? current : smallestSoFar; }

```

```
int smallest = accumulate(values.begin(), values.end(),
```

```
    <limits> numeric_limits<int>::max(), findLess);
```

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✧ **Clarity:**

With a customized for loop, you would have to read each line in the loop before you understood what the code did.

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require a predicate function: accepts an element and returns a bool
e.g. `bool isEven(int value) { return value %2 == 0; }`
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- ❖ **xxx_n** (generate_n, search_n, ...): performs a certain operation n times (on n elements in the container)
e.g. `fill_n(myDeque.begin(), 10, 0);`
`vector<int>::iterator it=search_n(myV.begin(), myV.end(), 2, 3);`
Two consecutive 3


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If an algorithm demands an Input iterator, it guarantees that the container pointed by the Input iterator is read-only by this algorithm.

Iterator Categories (cont'd)

Input Iterators

```
val = *itr;  
++itr;
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Iterator Categories (cont'd)

Random-Access Iterators

```
itr + distance;  
itr += distance; std::advance(itr, distance);  
itr1 < itr2; std::distance(itr1, itr2); itr2 - itr1;  
itr[myIndex]; *(itr + myIndex);
```

Bidirectional Iterators

```
--itr;
```

Forward Iterators

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*itr = val;  
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Reordering Algorithms

- ✧ **sort** // random-access iterators
 - ★ **sort(myVector.begin(), myVector.end());**
 - // i.e. vector or deque only, cannot sort list, set or map
 - // each element must provide **operator<** or **comparison function**
 - ★ ex. `bool compStrLen(const string &one, const string &two) { // or pass by value
 return one.length() < two.length();
}`
 - sort(myVector.begin(), myVector.end(), compStrLen);**

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- ❖ **stable_sort, partial_sort, partial_sort_copy, is_sorted, nth_element**
- ❖ **partition** // bidirectional iterators
 - ★ bool isOdd(int i) { return (i%2)==1; }
vector<int> myvector;
for (int i=1; i<10; ++i) myvector.push_back(i); // 1 2 3 4 5 6 7 8 9
vector<int>::iterator bound =
std::partition(myvector.begin(), myvector.end(), isOdd);

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// possible result: 1 9 3 7 5 6 4 8 2
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// i.e. vector or deque only, cannot sort list, set or map
// each element must provide **operator<** or **comparison function**
 - ★ ex. bool compStrLen(const string &one, const string &two) { // or pass by value
 return one.length() < two.length();
 }
 use pair to do multifield comparison
 sort(myVector.begin(), myVector.end(), compStrLen);
- ✧ **stable_sort, partial_sort, partial_sort_copy, is_sorted, nth_element**
- ✧ **partition** // bidirectional iterators
 - ★ bool isOdd(int i) { return (i%2)==1; }
vector<int> myvector;
for (int i=1; i<10; ++i) myvector.push_back(i); // 1 2 3 4 5 6 7 8 9
vector<int>::iterator bound =
 std::partition(myvector.begin(), myvector.end(), isOdd);
// possible result: 1 9 3 7 5 6 4 8 2
 bound ----->
 - ✧ **stable_partition, is_partitioned**

Reordering Algorithms (cont'd)

✧ **reverse**

// bidirectional iterators

★ **reverse(myVector.begin(), myVector.end());**

Reordering Algorithms (cont'd)

- ✧ **reverse** // bidirectional iterators
 - ★ **reverse(myVector.begin(), myVector.end());**
- ✧ **random_shuffle** // random-access iterators
 - ★ **random_shuffle(myVector.begin(), myVector.end());**


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- ✧ **shuffle** (C++11) // random-access iterators
 - ★ unsigned seed = std::chrono::system_clock::now().time_since_epoch().count();
★ **shuffle(myVec.begin(), myVec.end(), std::default_random_engine(seed));**


Reordering Algorithms (cont'd)

- ✧ **reverse** // bidirectional iterators
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 - ★ unsigned seed = std::chrono::system_clock::now().time_since_epoch().count();
shuffle(myVec.begin(), myVec.end(), std::default_random_engine(seed));
- ✧ **rotate** // forward iterators
 - ★ **rotate(v.begin(), v.begin()+2, v.end());** // begin, middle, end
// (0, 1, 2, 3, 4, 5) => (2, 3, 4, 5, 0, 1)

Reordering Algorithms (cont'd)

- ❖ **reverse** // bidirectional iterators
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- ❖ **next_permutation** // bidirectional iterators, operator<
 - * int v[] = {1, 4, 2};
* **next_permutation(v, v+3);** // (1, 4, 2) => (2, 1, 4)
 find next with carry

Reordering Algorithms (cont'd)

- ❖ **reverse** // bidirectional iterators
 - * **reverse(myVector.begin(), myVector.end());**
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 - * int v[] = {1, 4, 2};
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- ❖ **prev_permutation**  find next with carry

Other Utilities

✧ `min(a,b)`

- ★ return the smaller one of a and b

- ★ `cout << min(2,1) << ' ' << min(3.5, 2.1) << ' ' << min('d', 'b');` //1 2.1 b

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❖ `max(a,b)`

❖ `min_element`

// forward iterators, operator<

- ★ return the iterator of the smallest element in range [first, end)

- ★ `bool myfn(int i, int j) { return i<j; }`

```
struct { bool operator() (int i,int j) { return i<j; } } myobj;
```

```
int myints[] = {3,7,2,5,6,4,9};
```

```
cout << *min_element(myints,myints+7); // 2, operator<
```

```
cout << *min_element(myints,myints+7,myfn); // 2
```

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cout << *min_element(myints,myints+7,myobj); // 2
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```

❖ **merge**

// sorted range, input iterators, operator<

- ★ `int a[] = {10,5,15,25,20}; int b[] = {50,40,30,20,10}; vector<int> c(10);`

```
sort(a, a+5); sort(b, b+5);
```

```
merge(a, a+5, b, b+5, c.begin());
```

❖ **max(a,b)**

❖ **max_element**

Other Utilities

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```
sort(a, a+5); sort(b, b+5);
```

```
merge(a, a+5, b, b+5, c.begin());
```

// bidirectional iterators

// [first, middle) + [middle, last)

❖ **inplace_merge(first, middle, last)**

// sorted ranges, operator<

Other Utilities (cont'd)

✧ **set_union**

✧ **set_intersection**

✧ **bitset**

Other Utilities (cont'd)

✧ **set_union** // union of 2 **sorted** ranges, input iterators, operator<

✧ **set_intersection**

✧ **bitset**

Other Utilities (cont'd)

❖ **set_union** // union of 2 **sorted** ranges, input iterators, operator<

★ return an output iterator that is the end of the constructed sorted ranges

★ `int a[] = {10,5,15,25,20}; int b[] = {50,40,30,20,10}; vector<int> c(10);`

`sort(a, a+5); sort(b, b+5); // 5 10 15 20 25 30 40 50 0 0`

`vector<int>::iterator endIter = set_union(a, a+5, b, b+5, c.begin());`

`cout << *(endIter-1) << endl; // 50`

`c.resize(endIter-c.begin()); // 5 10 15 20 25 30 40 50`

❖ **set_intersection**

❖ **bitset**

Other Utilities (cont'd)

- ❖ **set_union** // union of 2 **sorted** ranges, input iterators, operator<
 - ★ return an output iterator that is the end of the constructed sorted ranges
 - ★

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vector<int>::iterator endIter = set_union(a, a+5, b, b+5, c.begin());
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c.resize(endIter-c.begin()); // 5 10 15 20 25 30 40 50
```
- ❖ **set_intersection** // intersection of 2 **sorted** ranges, input iterators, operator<
- ❖ **bitset**

Other Utilities (cont'd)

- ❖ **set_union** // union of 2 **sorted** ranges, input iterators, operator<
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`cout << *(endIter-1) << endl; // 50`
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`c.resize(endIter-c.begin()); // 10 20`
- ❖ **bitset**

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`c.resize(endIter-c.begin()); // 10 20`
- ❖ **bitset**
 - ★ `bitset<5> foo(string("01011"));`
`foo[0] = 0; /* LSB 01010 */ foo[1] = foo[0]; /* 01000 */`
`foo.flip(1); /* 01010 */ foo.flip(); /* 10101 */`
`cout << foo << ' ' << boolalpha << foo.test(3) << ' ' << foo.count() // 10101 false 3`

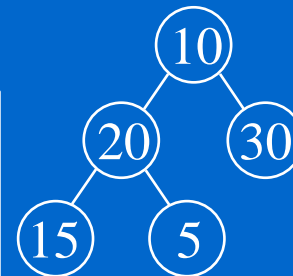
Max Heap

- ❖ Maintain a max heap in a vector or deque
 - ★ creation (heapify): **make_heap** // random-access iterators, **operator<**
 - ★ extract maximum: **pop_heap**
 - ✧ does not remove maximum element from the container
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 - ✧ does not return anything, use `v.front()` beforehand or use `v.back()` afterward
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```
int myints[] = {10,20,30,15, 5};  
vector<int> v(myints,myints+5);
```



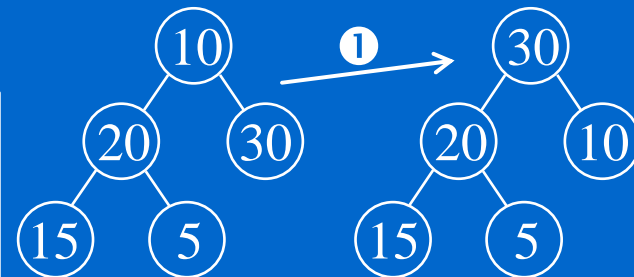
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vector<int> v(myints,myints+5);
```

❶ **make_heap**(v.begin(),v.end());

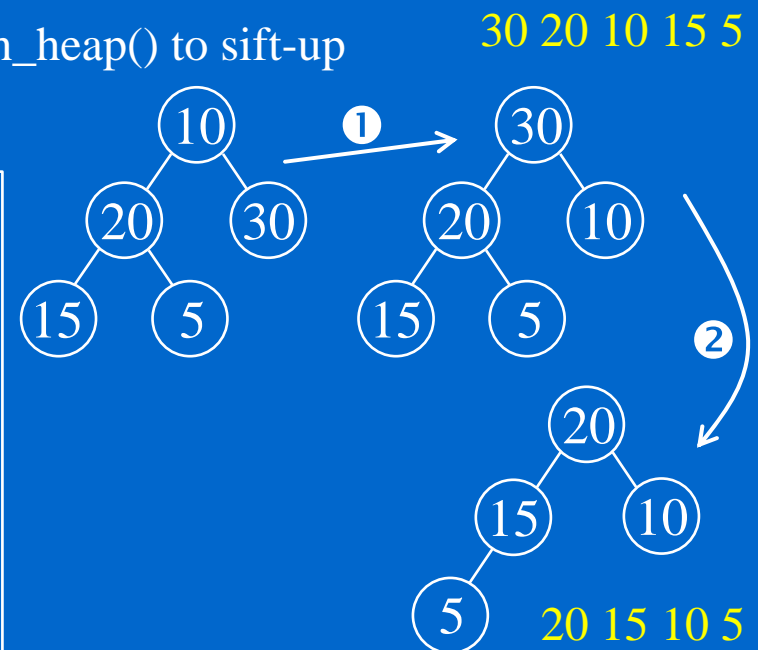


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int myints[] = {10,20,30,15, 5};  
vector<int> v(myints,myints+5);  
❶ make_heap(v.begin(),v.end());  
cout << v.front() << endl; // 30  
❷ pop_heap(v.begin(),v.end()); v.pop_back();
```



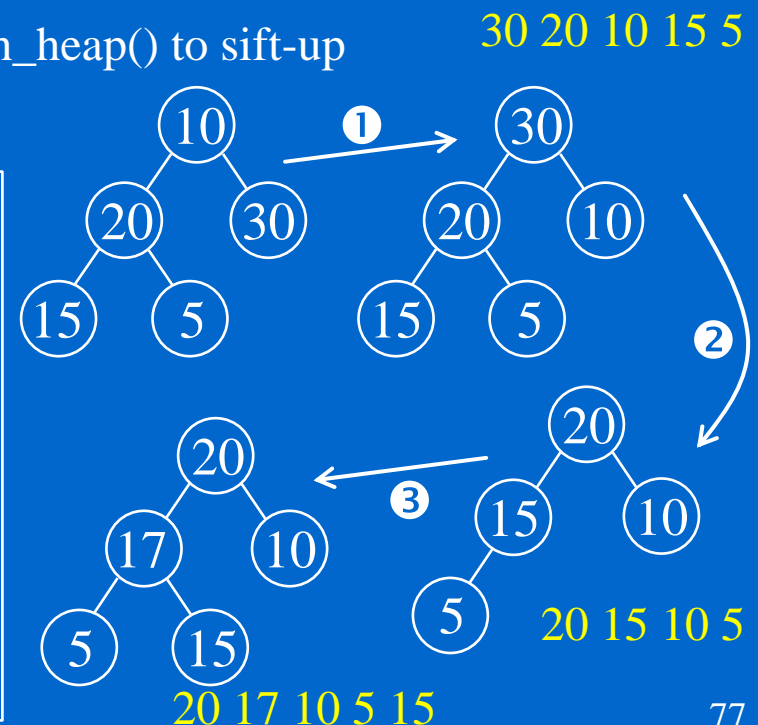
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vector<int> v(myints,myints+5);
```

- 1 **make_heap**(v.begin(),v.end());
cout << v.front() << endl; // 30
- 2 **pop_heap**(v.begin(),v.end()); v.pop_back();
- 3 v.push_back(17); **push_heap**(v.begin(),v.end())



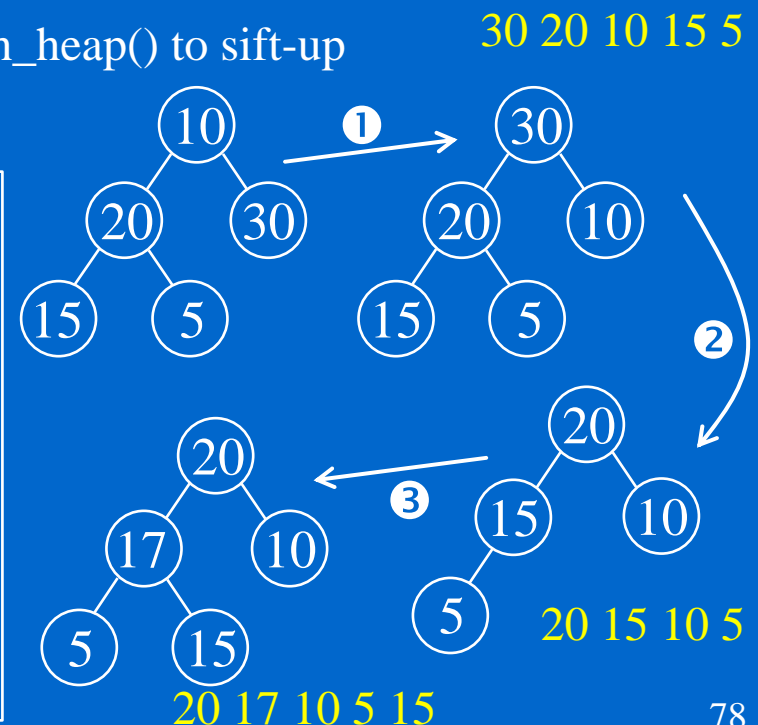
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sort_heap(v.begin(),v.end()); // no longer a heap



Max Heap

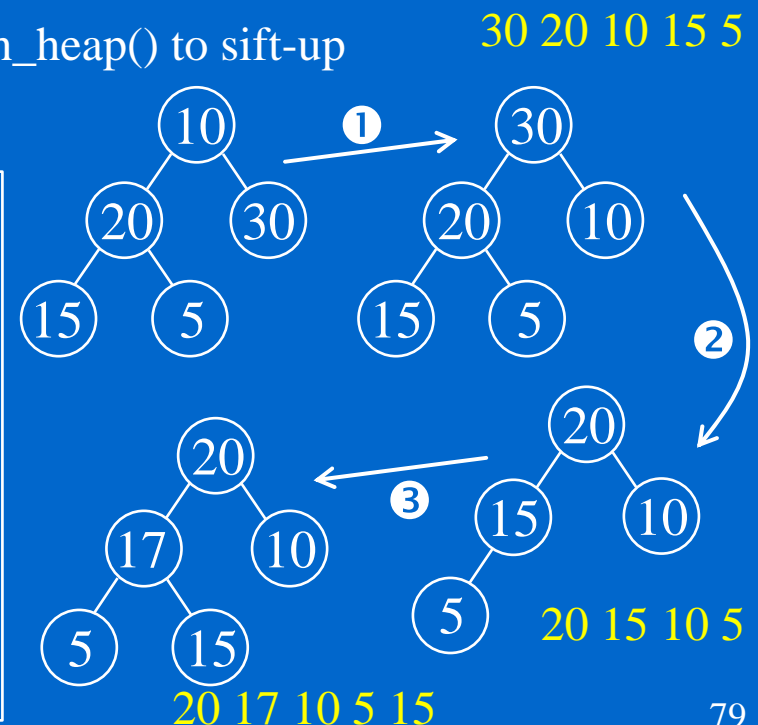
```
#include <queue>
std::priority_queue<int>
push()
empty(), top(), pop()
```

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Searching Algorithms

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❖ `bool binary_search(RandItr first, RandItr last, const Type& value)`

Searching Algorithms

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- ★ search for **value** in the designated **sorted** range, [**first**, **last**), delineating by two random-access iterators, i.e. iterators of vector or deque (map or set are sorted, their `find()` are efficient, i.e. log n)

Searching Algorithms

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 - ★ returns **last** iterator if nothing found
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avoid using find() on set or map, use set::find() or map::find() for efficiency
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Searching Algorithms (cont'd)

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- ✧ **ForwardItr lower_bound(ForwardItr first, ForwardItr last, const Type& value)**
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`else if (*itr == 137) ... // 137 is found`
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both algorithms are $O(\log n)$

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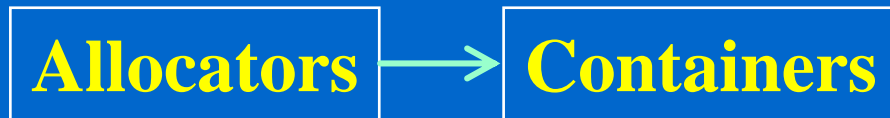
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e.g. (1,2,3,4,5) includes (2,4)

Six Parts of STL

Containers

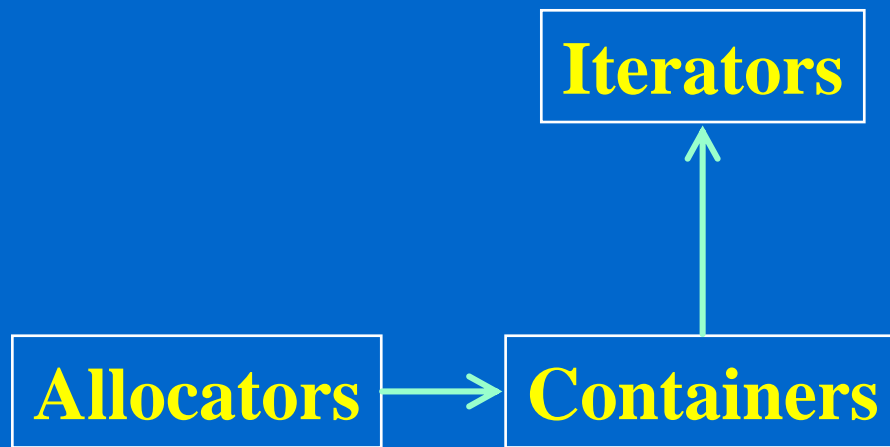
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Six Parts of STL



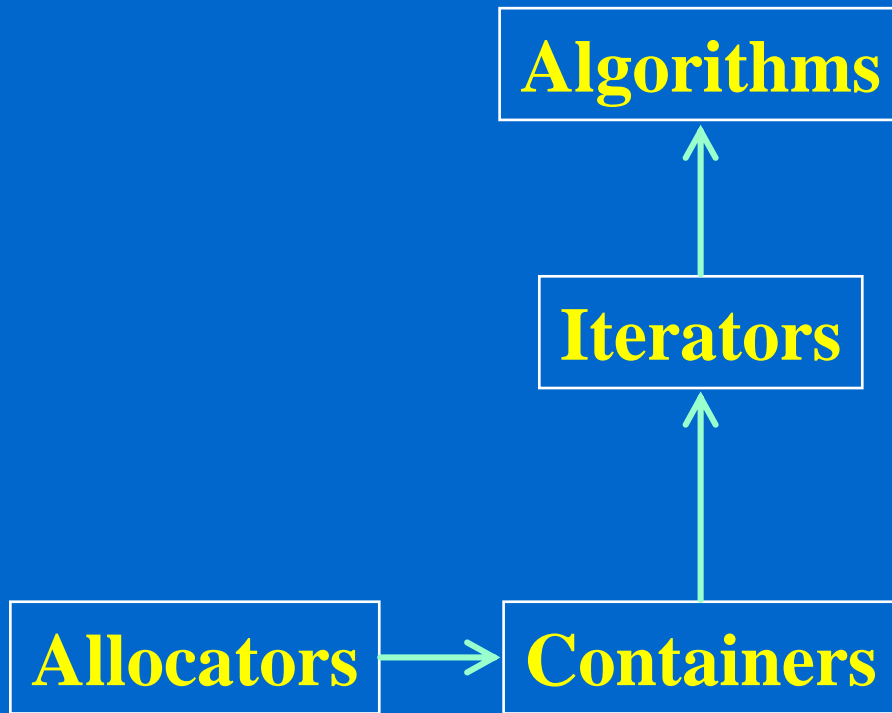
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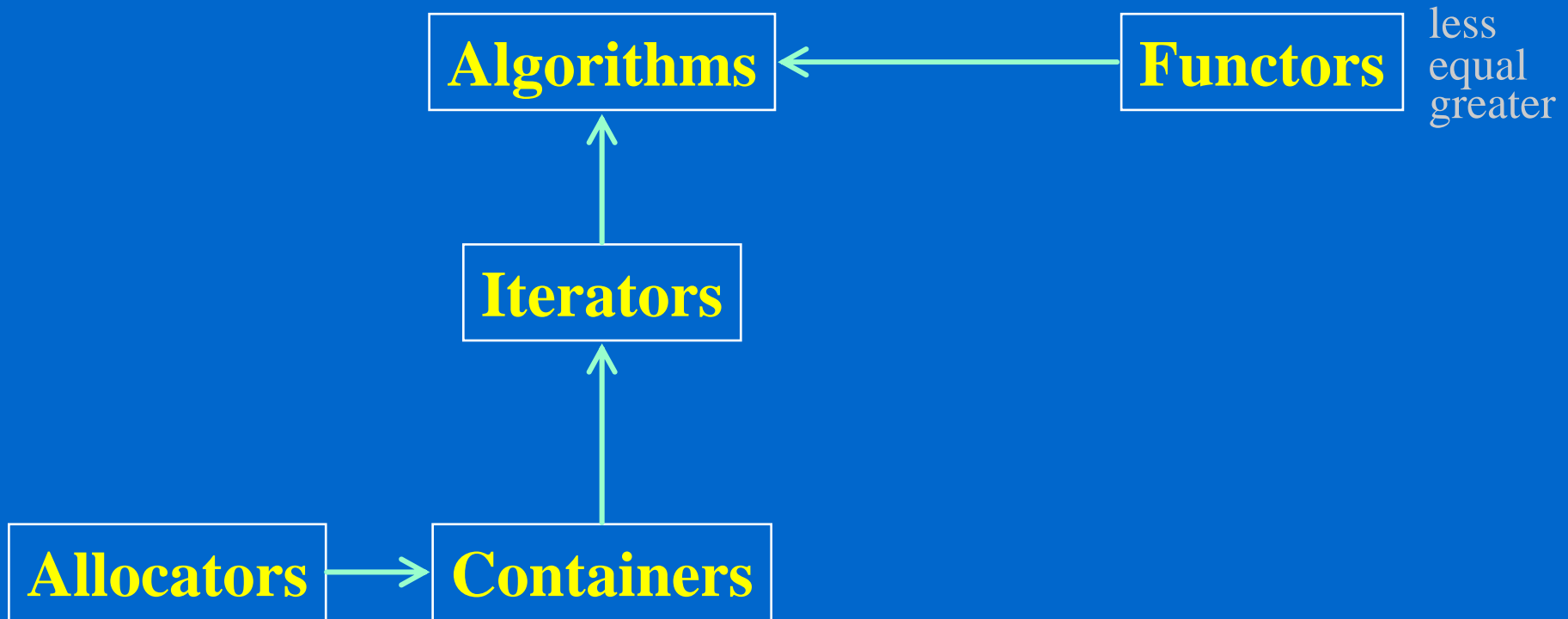
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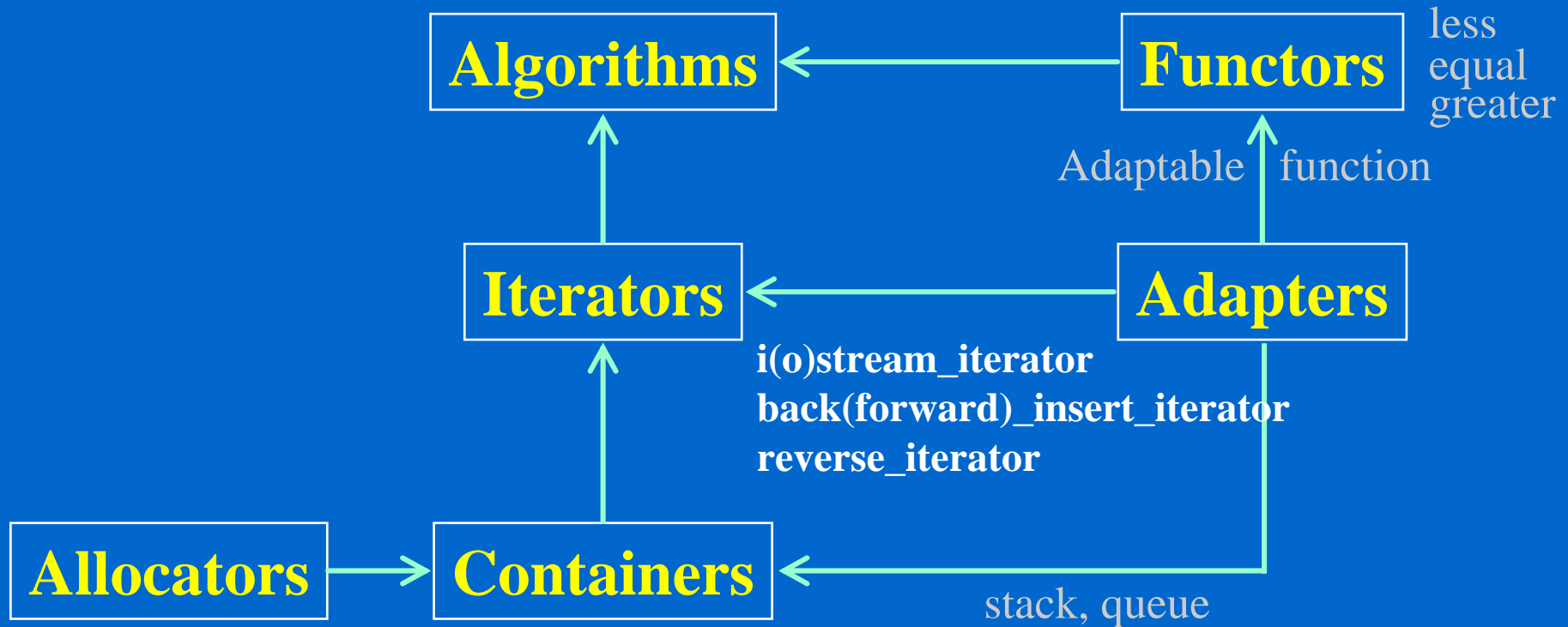
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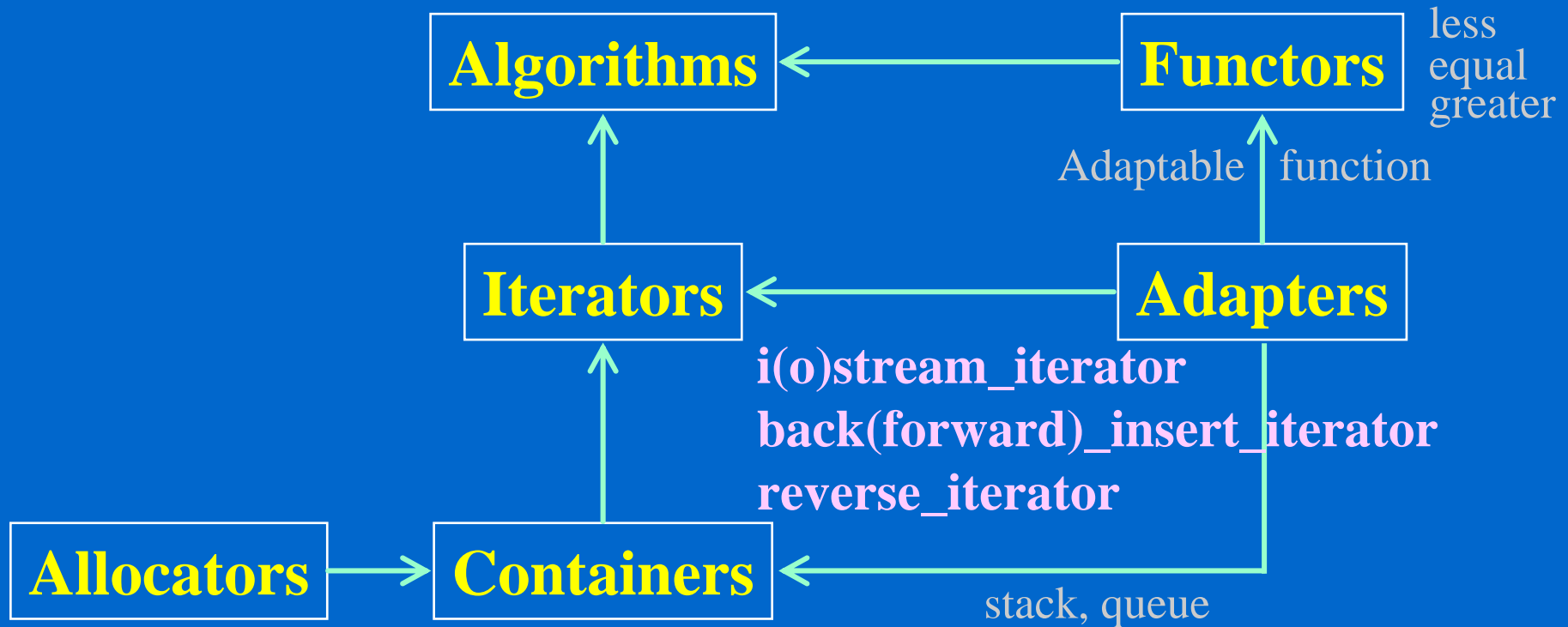
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ostream_iterator<int> myItr(cout, " "); *myItr = 123; myItr++;  
vector<int> myVec;  
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```
copy(istreambuf_iterator<char>(cin), istreambuf_iterator<char>(),  
      ostreambuf_iterator<char>(cout) ); // one line stream copy  
istream_iterator<int> itr(cin), endItr;  
int x; do x = *itr++, cout << x; while (itr!=endItr);
```

1 2 3 4^Z

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Note: **endItr** marks the end, is not attached to any input stream

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❖ vector<int> myVector; // no need to allocate space beforehand
  back_insert_iterator<vector<int> > itr(myVector);
  for (int i=0; i<10; ++i) *itr++ = i;
  int x[] = {10, 11, 12};
  reverse_copy(x, x+3, itr);
  // reverse_copy(x, x+3, back_insert_iterator<vector<int> >(myVector));
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vector, deque, list

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set<int> result;
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```
set_union(set1.begin(), set1.end(), set2.begin(), set2.end(),
```

```
    inserter(result, result.begin()));
```

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// the 2nd argument is an iterator pointing to the insertion point
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- ❖ Summary

```
back_insert_iterator<vector<int> > itr(myVector);  
back_insert_iterator<deque<char> > itr = back_inserter(myDeque);
```

Iterator Adaptors - <iterator>

- ❖ `set` does not support `front_insert_iterator` or `back_insert_iterator`, only supports `insert_iterator<Container> iter(container, iterator)`

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set<int> result;
```

```
set_union(set1.begin(), set1.end(), set2.begin(), set2.end(),
```

```
    inserter(result, result.begin()));
```

```
// the 2nd argument is an iterator pointing to the insertion point
```

```
// does not make sense for set or map, but is meaningful for vector, deque, or list
```

- ❖ Summary

```
back_insert_iterator<vector<int> > itr(myVector);
```

```
back_insert_iterator<deque<char> > itr = back_inserter(myDeque);
```

```
front_insert_iterator<deque<int> > itr(myIntDeque);
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formatted {

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formatted {

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formatted {

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Removal Algorithms

- ❖ Removal algorithms **do not remove** elements from containers; they only **shuffle down** all elements that need to be erased.
 - ★ They accept range specified by *iterators*, not *containers*, and thus do not know how to erase elements from containers.
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❖ ex1

```
int x[] = {218, 137, 130, 149, 137, 255};
vector<int> myvec;
copy(x, x+6, back_inserter(myvec));
myvec.erase(remove(myvec.begin(), myvec.end(), 137), myvec.end());
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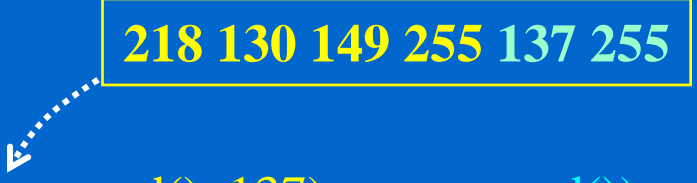
Output: **218 130 149 255**

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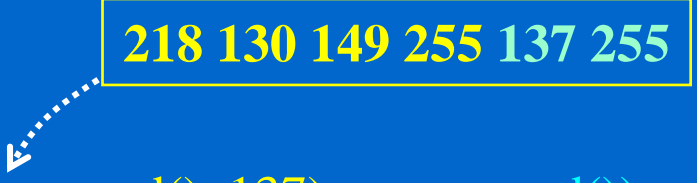
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Output: **218 130 149 255**

Note: `myvec.erase(myvec.end())` causes runtime error
`myvec.erase(myvec.end(), myvec.end())` is fine


empty range

Removal Algorithms

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❖ ex2

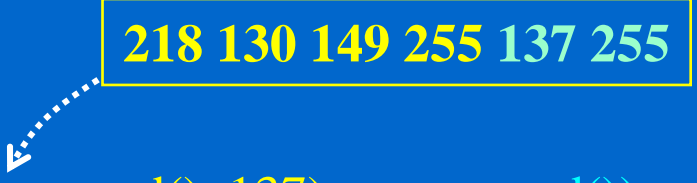
```
string stripPunctuation(string input) {
    input.erase(remove_if(input.begin(), input.end(), ::ispunct), input.end());
    return input;
}
```

Removal Algorithms

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Removal Algorithms (cont'd)


- ✧ **remove_copy, remove_copy_if**
 - ★ copy the elements that aren't removed into another container, operator==

Removal Algorithms (cont'd)

❖ `remove_copy`, `remove_copy_if`

- ★ copy the elements that aren't removed into another container, `operator==`

```
int myints[] = {10,20,30,30,20,10,10,20}; // 10 20 30 30 20 10 10 20
vector<int> myvector(8); // must ensure large enough
vector<int>::iterator iter =
remove_copy(myints, myints+8,
            myvector.begin(), // 10 30 30 10 10 0 0 0
            20);
myvector.erase(iter, myvector.end()); // 10 30 30 10 10
```




Removal Algorithms (cont'd)

❖ `remove_copy`, `remove_copy_if`

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❖ `unique_copy`


- ❖ returns an iterator pointing to the end of the copied range, which contains no **consecutive** duplicates.

Removal Algorithms (cont'd)

❖ `remove_copy`, `remove_copy_if`

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- ❖ returns an iterator pointing to the end of the copied range, which contains no **consecutive** duplicates.

```
int myints[] = {10,20,20,20,30,30,20,20,10};
vector<int> myvector(9); // 0 0 0 0 0 0 0 0 0
vector<int>::iterator iter =
unique_copy(myints, myints+9, myvector.begin()); // 10 20 30 20 10 0 0 0 0
```

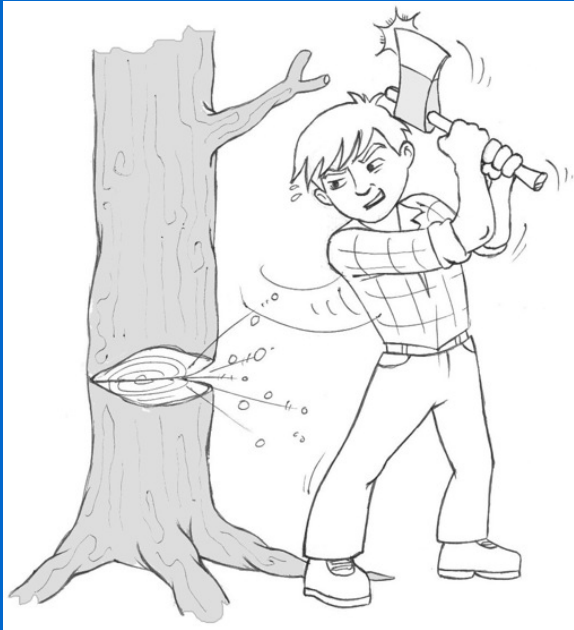


Functional Thinking

- ✧ Note: You are not going to master STL <algorithm>, <numeric>, <iterator>, or <functional> through your *procedural* or *object-oriented* intuitions!!!

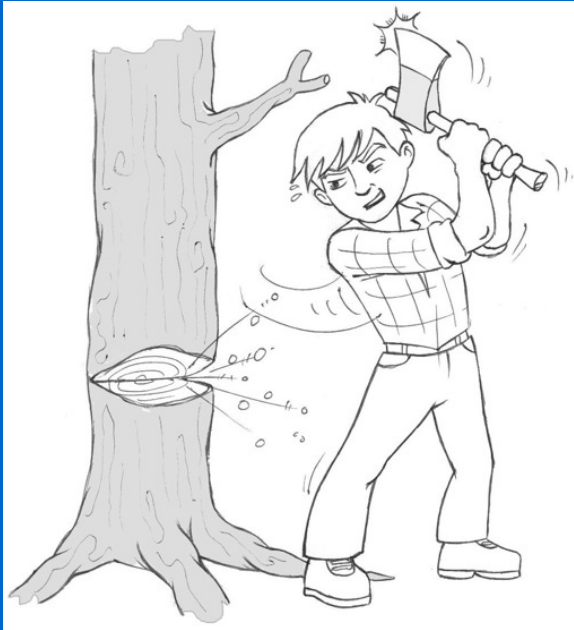
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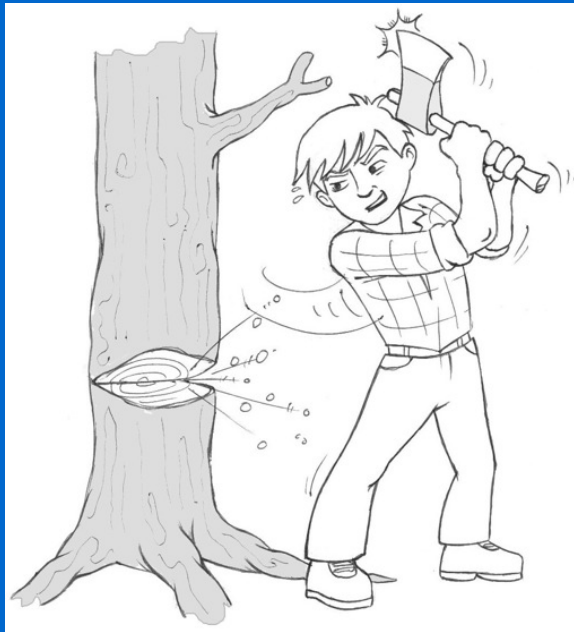
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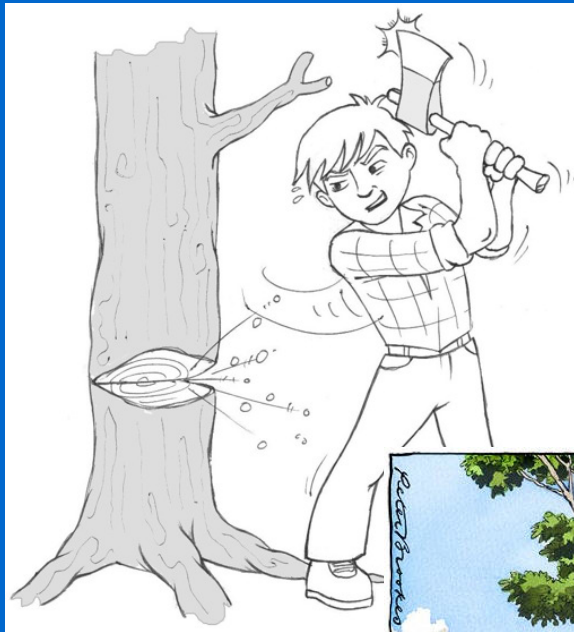
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Can you figure out the way to use a chainsaw in place of the ax if what you ever seen is an ax in working!!!!

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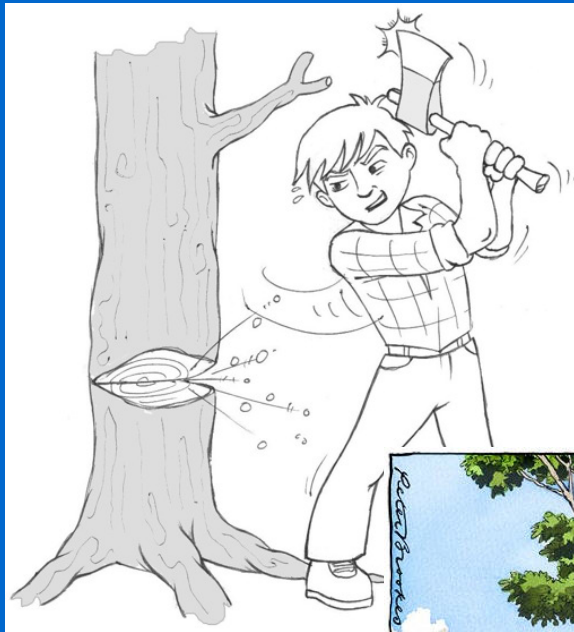


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Paradigm shift!!!

Functional Thinking (cont'd)

- ✧ *Functional Thinking: Paradigm over Syntax*, Neal Ford, 2014

Functional Thinking (cont'd)

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Stop thinking of low-level details of implementation and start focusing on the problem domain and on the results across steps (gradual transformation of input data toward the results)

Functional Thinking (cont'd)

- ✧ Michael Feather

- OO makes codes understandable by encapsulating moving parts,
 - FP makes codes understandable by removing moving parts.

Functional Thinking (cont'd)

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 - OO makes codes understandable by encapsulating moving parts,
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Languages adopting FP paradigms: Perl, PHP, Ruby on Rail, JavaScript,
Python, R, C#, and C++

Again, why going FP?

✧ Cloud computing: **Google Map/Reduce**

Again, why going FP?

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Big Data: Statistics Computing Language – R

Again, why going FP?

- ✧ **Cloud computing: Google Map/Reduce**
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- ✧ **Cool !!!**
- ✧ **Fashion !!!**

Again, why going FP?

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- Big Data: Statistics Computing Language – R**
- ✧ **Cool !!!**
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 the real motivation is **paralellism:**
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 - ★ GPU and Heterogeneous Computing
 - ★ Cloud and Distributed computing

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Inherent **immutability** of Functional programming is a very good starting point for exploiting H/W parallelism.

Map / Filter / Reduce

STL

Functional Language

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Functional Language

- ❖ transform() --- **map** in Scala or Closure
- copy() collect in Groovy
- for_each()
- replace()
- sort()
- partition()

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Functional Language

- ✧ transform() --- **map** in Scala or Closure
 - copy() collect in Groovy
 - for_each()
 - replace()
 - sort()
 - partition()
- ✧ remove() + erase() --- **filter** in Scala or Closure
- ✧ accumulate() --- **reduce** in Scala or Closure
 - count() convert
 - equal()
 - search() collect in Java8
 - selection() inject, join in Groovy
 - min_element() fold in Functional Java

Mapping algorithms

- ❖ **transform**: applies a function to a range of elements and stores the result in the specified destination range

```
string convertToLowerCase(string text) {  
    transform(text.begin(), text.end(), text.begin(), ::tolower);  
    return text;  
}
```

Mapping algorithms

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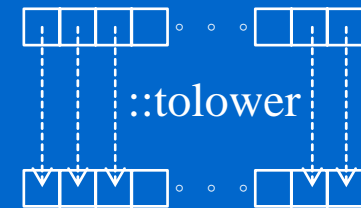
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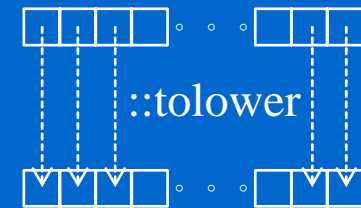


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```

inplace

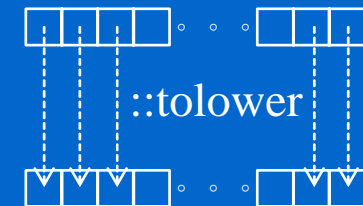


Mapping algorithms

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```
string convertToLowerCase(string text) {  
    transform(text.begin(), text.end(), text.begin(), ::tolower);  
    return text;  
}
```

inplace



```
int toInt(int ch) { return ch >= 'a' ? ch - 'a' : ch - 'A' ; }  
string convertToInteger(string text, vector<int> &dest) {  
    transform(text.begin(), text.end(), back_inserter(dest), toInt);  
    return text;  
}
```

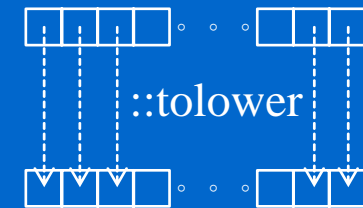
the result could be another type

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string convertToLowerCase(string text) {  
    transform(text.begin(), text.end(), text.begin(), ::tolower);  
    return text;  
}
```

inplace



```
int toInt(int ch) { return ch>='a' ? ch - 'a' : ch - 'A' ; }  
string convertToInteger(string text, vector<int> &dest) {  
    transform(text.begin(), text.end(), back_inserter(dest), toInt);  
    return text;  
}
```

the result could be another type

- ❖ **for_each**: applies a function to a range of elements

```
void toLower(int &ch) { ch = ch<='Z' ? ch - 'A' + 'a' : ch; }  
string convertToLowerCase(string text) {  
    for_each(text.begin(), text.end(), toLower);  
    return text;  
}
```

the result is of the same type

Mapping algorithms (cont'd)

- ✧ `replace(ForwardItr start, ForwardItr end,
const Type & toReplace, const Type& replaceWith)`

Mapping algorithms (cont'd)

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```
int myints[] = {10, 20, 30, 30, 20, 10, 10, 20};  
vector<int> myvector(myints, myints+8);           // 10 20 30 30 20 10 10 20  
replace(myvector.begin(), myvector.end(), 20, 99); // 10 99 30 30 99 10 10 99
```

Mapping algorithms (cont'd)

- ❖ `replace(ForwardItr start, ForwardItr end, const Type & toReplace, const Type& replaceWith)`

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int myints[] = {10, 20, 30, 30, 20, 10, 10, 20};  
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- ❖ `replace_if(ForwardItr start, ForwardItr end, Predicate fn, const Type& replaceWith)`

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```

- ❖ **replace_if**(ForwardItr start, ForwardItr end,
Predicate fn, const Type& replaceWith)

```
bool isOdd (int i) { return ((i%2)==1); }  
int myints[] = {10, 11, 30, 30, 13, 10};  
vector<int> myvector(myints, myints+8);           // 10 11 30 30 13 10  
replace_if(myvector.begin(), myvector.end(), isOdd, 0); // 10 0 30 30 0 10
```

Mapping algorithms (cont'd)

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const Type & toReplace, const Type& replaceWith)

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- ❖ **generate**(ForwardItr start, ForwardItr end, Generator fn)

```
int randomNumber() { return (std::rand()%100); }  
srand(unsigned(std::time(0))); vector<int> myvector(8);  
generate(myvector.begin(), myvector.end(), randomNumber);
```


Mapping algorithms (cont'd)

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srand(unsigned(std::time(0))); vector<int> myvector(8);  
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```

- ❖ **generate_n**(OutputItr start, size_t n, Generator fn)

for_each

```
#include <iostream>
#include <algorithm>
using namespace std;
template <class T>
class print {
public:
    print(ostream &os)
        : m_os(os), m_count(0) {}
    void operator()(const T &t) {
        m_os << t << ' ';
        ++m_count;
    }
    int count() { return m_count; }
private:
    ostream &m_os;
    int m_count;
};
```

```
int main()
{
    int array[] = {1, 4, 2, 8, 5, 7};
    const int n = sizeof(array) / sizeof(int);

    print<int> f =
        for_each(array, array+n, print<int>(cout));
    cout << endl << f.count()
        << " objects printed." << endl;

    return 0;
}
```

STL Abstractions

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Algorithms (customized with the **plugged-in function objects**) are abstract mechanisms that focus on solving the general structure of a problem instead of the particular container or the specific data type in the container.

Things to Remember

when using STL algorithms

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❖ *Ensure a **container's size** is large enough to accept all components being transferred into it.*

e.g. `vector<int> v; back_insert_iterator<vector<int> > iter(v);`

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bool IsPalindrome(string input) {  
    for (int k=0; k<input.size()/2; ++k)  
        if (input[k]!=input[input.length()-1-k])  
            return false;  
    return true;  
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- ❖ 1st STL version

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bool IsPalindrome(string input) {  
    string reversed = input;  
    reverse(reversed.begin(), reversed.end());  
    return reversed == input;  
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```
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reverse_copy(input.begin(),  
             input.end(),  
             reversed);  
return reversed == input;
```

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```
string reversed;  
reverse_copy(input.begin(),  
             input.end(),  
             reversed);  
return reversed == input;
```

plain, narrative, but less efficient

Palindrome (cont'd)

- ❖ 2nd STL version: use **reverse_iterator** and **equal**

```
bool IsPalindrome(string input) {  
    return equal(input.begin(), input.begin()+input.size()/2, input.rbegin());  
}
```

Palindrome (cont'd)

- ❖ 2nd STL version: use **reverse_iterator** and **equal**

```
bool IsPalindrome(string input) {  
    return equal(input.begin(), input.begin()+input.size()/2, input.rbegin());  
}
```

- ❖ More: stripping out everything except alphabetic char

```
#include <cctype> // isalpha()  
#include <algorithm> // remove_if(), equal()  
bool IsNotAlpha(char ch) {  
    return !isalpha(ch);  
}  
bool IsPalindrome(string input) {  
    input.erase(remove_if(input.begin(), input.end(), IsNotAlpha), input.end());  
    return equal(input.begin(), input.begin()+input.size()/2, input.rbegin());  
}
```


Word Palindrome

- ❖ Basic steps

1. Strip out everything except letters and spaces, convert to uppercase

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```
bool IsNotAlphaOrSpace(char ch) { return !isalpha(ch) && !isspace(ch); }
bool IsWordPalindrome(string input)
{
    input.erase(remove_if(input.begin(), input.end(), IsNotAlphaOrSpace),
                input.end());
    transform(input.begin(), input.end(), input.begin(), ::toupper);
    stringstream tokenizer(input);
    vector<string> tokens;
    tokens.insert(tokens.begin(), istream_iterator<string>(tokenizer),
                  istream_iterator<string>());
    return equal(tokens.begin(), tokens.begin()+tokens.size()/2, tokens.rbegin());
}
```

Word Palindrome

❖ Basic steps

1. Strip out everything except letters and spaces, convert to uppercase
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bool IsNotAlphaOrSpace(char ch) { return !isalpha(ch) && !isspace(ch); }
bool IsWordPalindrome(string input)
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    input.erase(remove_if(input.begin(), input.end(), IsNotAlphaOrSpace),
                input.end());
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    stringstream tokenizer(input);
    vector<string> tokens;
    tokens.insert(tokens.begin(), istream_iterator<string>(tokenizer),
                  istream_iterator<string>());
    return equal(tokens.begin(), tokens.begin()+tokens.size()/2, tokens.rbegin());
}
```

Clang or GNU g++ has tolower()/toupper() in <locale> header also

<cctype>

<code>int isalnum(int c)</code>	Check if character is alphanumeric
<code>int isalpha(int c)</code>	Check if character is alphabetic
<code>int isblank(int c)</code>	Check if character is blank (C++11)
<code>int iscntrl(int c)</code>	Check if character is a control character
<code>int isdigit(int c)</code>	Check if character is decimal digit
<code>int isgraph(int c)</code>	Check if character has graphical representation
<code>int islower(int c)</code>	Check if character is lowercase letter
<code>int isprint(int c)</code>	Check if character is printable
<code>int ispunct(int c)</code>	Check if character is a punctuation character
<code>int isspace(int c)</code>	Check if character is a white-space
<code>int isupper(int c)</code>	Check if character is uppercase letter
<code>int isxdigit(int c)</code>	Check if character is hexadecimal digit
<code>int isalnum(int c)</code>	Check if character is alphanumeric
<code>int isalpha(int c)</code>	Check if character is alphabetic
<code>int tolower(int c)</code>	Convert uppercase letter to lowercase
<code>int toupper(int c)</code>	Convert lowercase letter to uppercase

In C++, a locale-specific **template** version of each function exists in header <locale> use `::isalnum()` to specify `isalnum()` in `cctype`

<cmath>

❖ Trigonometric functions

<code>double cos(double)</code>	Compute cosine
<code>double sin(double)</code>	Compute sine
<code>double tan(double)</code>	Compute tangent
<code>double acos(double)</code>	Compute arc cosine
<code>double asin(double)</code>	Compute arc sine
<code>double atan(double)</code>	Compute arc tangent
<code>double atan2(double)</code>	Compute arc tangent with two parameters

❖ Hyperbolic functions

<code>double cosh(double)</code>	Compute hyperbolic cosine
<code>double sinh(double)</code>	Compute hyperbolic sine
<code>double tanh(double)</code>	Compute hyperbolic tangent
<code>double acosh(double)</code>	Compute arc hyperbolic cosine (C++11)
<code>double asinh(double)</code>	Compute arc hyperbolic sine (C++11)
<code>double atanh(double)</code>	Compute arc hyperbolic tangent (C++11)

❖ Exponential and logarithmic functions

double exp(double x)	Compute exponential function, e^x
double frexp(double x, int* exp)	Get significand and exponent, $x = \text{sign} * 2^{\text{exp}}$
double ldexp(double x, int exp)	$x * 2^{\text{exp}}$
double log(double x)	Compute natural logarithm, w.r.t. Euler number e
double log10(double x)	Compute common logarithm
double modf(double x, double* intpart)	Break into fractional and integral parts
double exp2(double x), exp2l(x)	Compute 2^x (C++11)
double expm1(double x), expm1l(x)	Compute $e^x - 1$ (C++11)
int ilogb(double x)	Integer binary logarithm (C++11)
int ilogb(long double x)	Returns the integral part of the logarithm of $ x $, using FLT_RADIX ($=2$) as base
double log1p(double x)	Compute logarithm plus one, $\log(x+1)$ (C++11)
double log2(double x)	Compute binary logarithm (C++11)
double logb(double x)	Compute floating-point base logarithm, $\log x $ using FLT_RADIX ($=2$) as base (C++11)
double scalbn(double x, int n)	$\text{scalbn}(x, n) = x * \text{FLT_RADIX}^n$ (C++11)

❖ Power functions

<code>double pow(double base, double exp)</code>	Raise to power, base^{exp}
<code>double sqrt(double x)</code>	Compute square root
<code>double cbrt(double x)</code>	Compute cubic root (C++11)
<code>double hypot(double x, double y)</code>	Compute hypotenuse (C++11)

❖ Error and gamma functions

<code>double erf(double x)</code>	Compute error function (C++11)
<code>double erfc(double x)</code>	Compute complementary error function (C++11)
<code>double tgamma(double x)</code>	Compute gamma function (C++11)
<code>double lgamma(double x)</code>	Compute log-gamma function (C++11)

❖ Rounding and remainder: `ceil`, `floor`, `fmod`, `trunc`, `round`, `lround`, `llround`, `rint`, `lrint`, `llrint`, `nearbyint`, `remainder`, `remquo`

❖ Floating-point manipulation: `copysign`, `nan`, `nextafter`, `nexttoward`

❖ Minimum, maximum, difference: `fdim`, `fmax`, `fmin`

❖ Other: `fabs`, `abs`, `fma`

❖ Classification: `fpclassify`, `isfinite`, `isinf`, `isnan`, `isnormal`, `signbit`

❖ Comparison: `isgreater`, `isgreaterequal`, `isless`, `islessequal`, `islessgreater`, `isunordered`

❖ Constants: `INFINITY`, `NAN`, `HUGE_VAL`

Boost

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- ❖ **Boost** ==> **C++TR1** (Library extension to C++03) ==> **C++11**
 - ★ **smart_ptrs** – manage the lifetime of referred object with reference counting (shared_ptr, shared_array, scoped_ptr, scoped_array, weak_ptr, intrusive_ptr)
 - ★ boost::**lambda**, boost::**function**, boost::**bind** – higher order programming
 - ★ boost::**regex** – regular expression
 - ★ boost::**asio** – blocking/non-blocking wait with timers, multithreading, socket
 - ★ **FileSystem** – system independent file size, attributes, existence, directory traversal, path handling
 - ★ template metaprogramming (boost::**mpl**)

Boost

- ❖ **Boost**, an excellent open source C++ libraries, provides lots of useful facilities not available in STL before C++11.
- ❖ **Boost** ==> **C++TR1** (Library extension to C++03) ==> **C++11**
 - ★ **smart_ptrs** – manage the lifetime of referred object with reference counting (shared_ptr, shared_array, scoped_ptr, scoped_array, weak_ptr, intrusive_ptr)
 - ★ boost::**lambda**, boost::**function**, boost::**bind** – higher order programming
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Documents of Boost provide excellent in-depth discussions of the design decisions, constraints, and requirements that went into constructing the library.

Magic Square Solver (1/4)

- ✧ A “magic square” is a 3x3 grid in which all elements are distinct and all 3 elements in every row, column, and diagonal sum to the same number, e.g.

2	7	6
9	5	1
4	3	8

```
vector<int> magicSquare(9);  
for (i=0; i<9; ++i) magicSquare[i]=i+1;
```

```
do {  
    outputConfig(magicSquare);  
}  
while (next_permutation(magicSquare.begin(), magicSquare.end()));
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$$2+7+6=15$$

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- ✧ Use next_permutation() to generate all configurations

```
do {  
    outputConfig(magicSquare);  
}  
while (next_permutation(magicSquare.begin(), magicSquare.end()));
```


Magic Square Solver (2/4)

✧ Output a configuration

```
for (i=0; i<3; ++i)
    copy(magicSquare.begin()+3*i, magicSquare.begin()+3*i+3,
         ostream_iterator<int>(cout, " ")), cout << endl;
```

```
const int starts[] = {0, 3, 6, 0, 1, 2, 2, 0};
const int offsets[] = {1, 1, 1, 3, 3, 3, 2, 4};
for (i=0; i<8; ++i)
    for (sums[i]=0, j=0; j<3; ++j)
        sums[i] += magicSquare[starts[i]+j*offsets[i]];
```

```
if (8==count(sums, sums+8, 15))
    outputConfig(magicSquare);
```

Magic Square Solver (2/4)

- ❖ Output a configuration

```
for (i=0; i<3; ++i)
    copy(magicSquare.begin()+3*i, magicSquare.begin()+3*i+3,
         ostream_iterator<int>(cout, " ")), cout << endl;
```

- ❖ Use **for loop** to evaluate everyone of the 8 conditions

```
const int starts[] = {0, 3, 6, 0, 1, 2, 2, 0};
const int offsets[] = {1, 1, 1, 3, 3, 3, 2, 4};
for (i=0; i<8; ++i)
    for (sums[i]=0, j=0; j<3; ++j)
        sums[i] += magicSquare[starts[i]+j*offsets[i]];
```

```
if (8==count(sums, sums+8, 15))
    outputConfig(magicSquare);
```

Magic Square Solver (2/4)

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    for (sums[i]=0, j=0; j<3; ++j)
        sums[i] += magicSquare[starts[i]+j*offsets[i]];
```

- ❖ Use **count()** to validate the conjunction of all 8 conditions

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if (8==count(sums, sums+8, 15))
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```

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 - ⤴ It is necessary to config the predicate with different ways of accumulation.

use a **functor**

```
for (i=0; i<8; ++i)
    sums[i] = accumulate(magicSquare.begin(), magicSquare.end(), 0,
                        Constraint(starts[i],offsets[i]));
```

Magic Square Solver (4/4)

```
class Constraint {  
public:  
    Constraint(const int start, const int offset)  
        : index(0), x1(start), x2(start+offset), x3(start+2*offset) {}  
    int operator()(int sum, int value) {  
        if (index==x1||index==x2||index==x3)  
            sum += value;  
        index++;  
        return sum;  
    }  
private:  
    int index;  
    const int x1, x2, x3;  
};
```

Magic Square Solver (4/4)

```
class Constraint {
```

```
public:
```

```
    Constraint(const int start, const int offset)
```

```
        : index(0), x1(start), x2(start+offset), x3(start+2*offset) {}
```

```
    int operator()(int sum, int value) {
```

```
        if (index==x1||index==x2||index==x3)
```

```
            sum += value;
```

```
            index++;
```

```
            return sum;
```

```
    }
```

```
private:
```

```
    int index;
```

```
    const int x1, x2, x3;
```

```
};
```

Magic Square Solver (4/4)

```
class Constraint {
```

```
public:
```

```
    Constraint(const int start, const int offset)
```

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        : index(0), x1(start), x2(start+offset), x3(start+2*offset) {}
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    int operator()(int sum, int value) {
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        if (index==x1||index==x2||index==x3)
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            return sum;
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    }
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    int index;
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Monoalphabetic Substitution Cipher

- ✧ A monoalphabetic substitution cipher is a simple form of encryption, where each of the 26 letters are mapped to another letter exclusively in the alphabet.

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---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

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encryption ↓

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- ★ Use **random_shuffle** to generate a map as the encoding codebook and a map as the decoding codebook

```
int encTable[26], decTable[26]; // two direct address tables (DAT)
random_shuffle(encTable, encTable+26);
for (i=0; i<26; i++) decTable[encTable[i]] = i;
```

Substitution Cipher (cont'd)

- ★ Config **transform** with a decryption **functor**, which takes a decoding codebook and maps a ciphertext character to a plaintext character.

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```
class mapping {  
  public:  
    mapping(int table[]): DAT(table) {}  
    char operator()(char &source) { return 'A'+DAT[source-'A']; }  
  private:  
    int *DAT;  
};
```

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};
```

```
transform(plaintext1.begin(), plaintext1.end(),  
          back_inserter(ciphertext), mapping(encTable));
```

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```
transform(ciphertext.begin(), ciphertext.end(),  
          back_inserter(plaintext2), mapping(decTable));
```

pair<T1, T2>

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```
bool operator<(pair<T1,T2>& rhs) {  
    if (first<rhs.first) return true;  
    else if ((first==rhs.first)&&(second<rhs.second)) return true;  
    else return false; // *this >= rhs  
}
```

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```

- ✧ e.g. **multi-field sorting** on **pair<string, pair<int, vector<int>>>**

```
vector<pair<string, pair<int, vector<int>>>> v;  
... // populate the vector v with data;  
sort(v.begin(), v.end());
```

Convenient Aliases

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typedef vector<int> vi;
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A two-dimensional 10x20 array initialized with 0
`vvi matrix(10, vi(20, 0))`

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```
typedef vector<vii> vvii;
```

```
#define sz(a) int((a).size())
```

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typedef vector<int> vi;  
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#define pb push_back
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typedef vector<int> vi;  
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typedef vector<string> vs;  
typedef vector<ii> vii;  
typedef vector<pair<double, ii> > vdii;  
typedef vector<vii> vvii;  
  
#define sz(a) int((a).size())  
#define pb push_back  
#define all(c) (c).begin(),(c).end()
```

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#define sz(a) int((a).size())  
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```

```
#define tr(c,i) for(typeof((c).begin()) i = (c).begin(); i != (c).end(); i++)
```

only for GNU g++



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typedef vector<int> vi;  
typedef vector<vi> vvi;  
typedef pair<int,int> ii;  
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```
#define sz(a) int((a).size())  
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#define tr(c,i) for(typeof((c).begin()) i = (c).begin(); i != (c).end(); i++)  
#define has(c,x) ((c).find(x) != (c).end())
```

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```

```
#define tr(c,i) for(typeof((c).begin() i = (c).begin(); i != (c).end(); i++)
```

```
#define has(c,x) ((c).find(x) != (c).end())
```

```
#define hasG(c,x) (find(all(c),x) != (c).end())
```

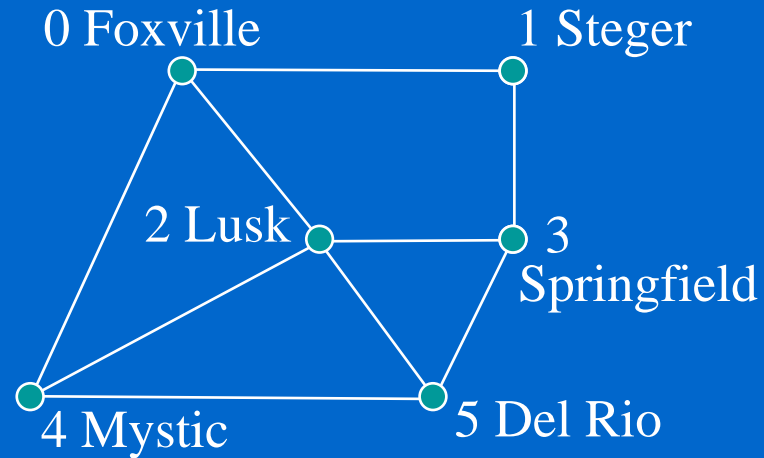
A two-dimensional 10x20 array initialized with 0
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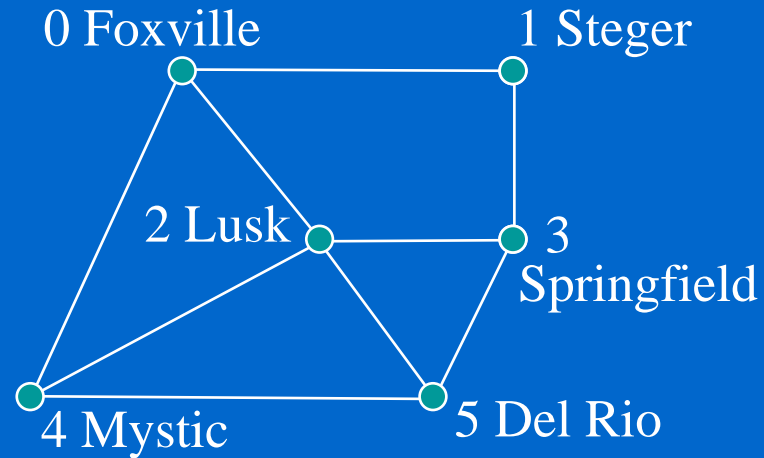
Graph Connectivity - DFS

❖ Depth-First Search



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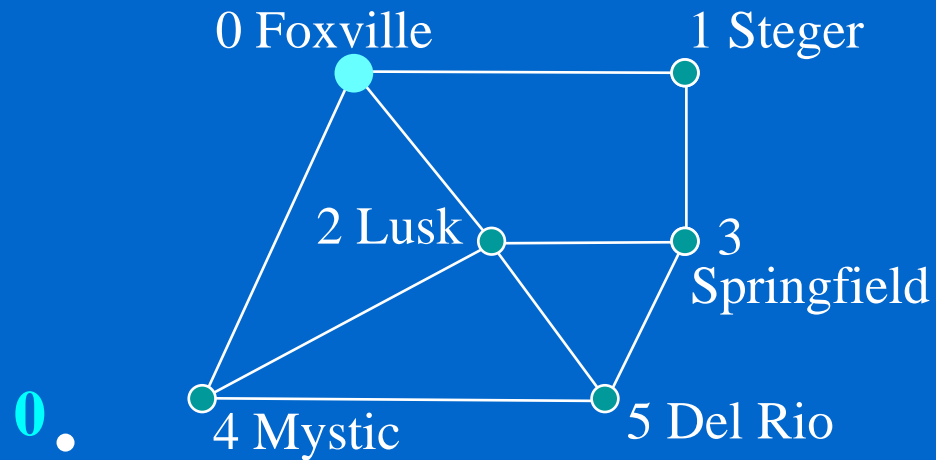


visited

0	1	2	3	4	5
0	0	0	0	0	0

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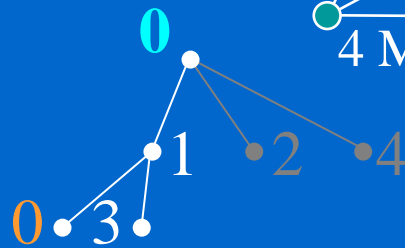
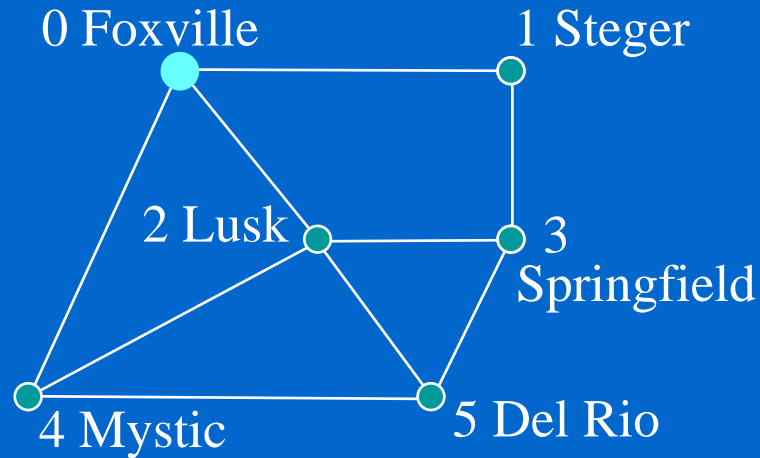


visited

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1	1	0	0	0	0

Graph Connectivity - DFS

✧ Depth-First Search

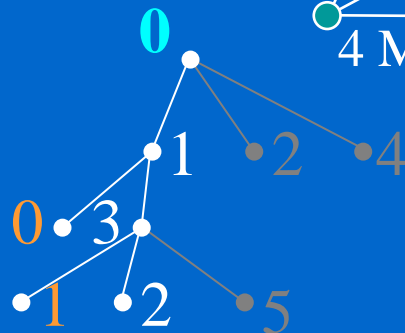
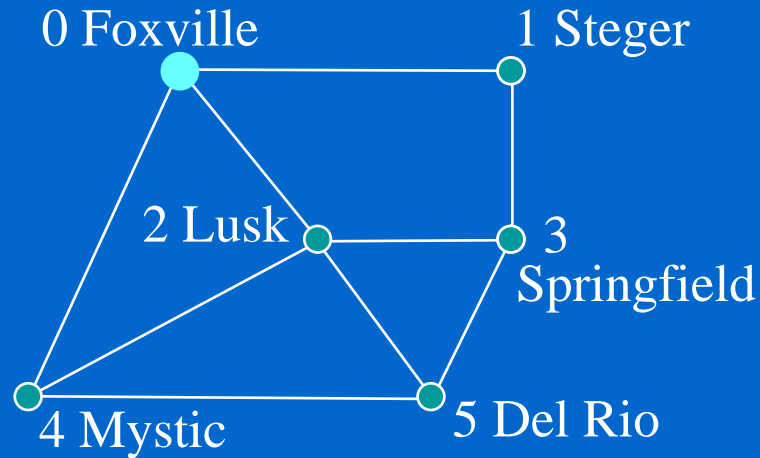


visited

0	1	2	3	4	5
1	1	0	1	0	0

Graph Connectivity - DFS

✧ Depth-First Search

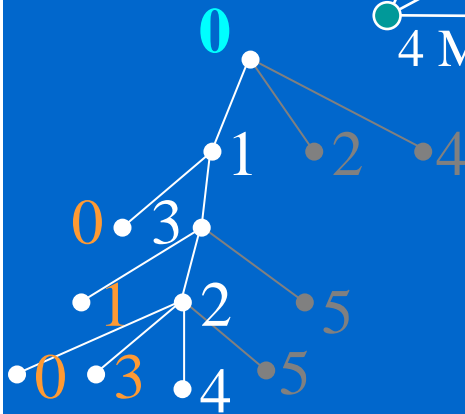
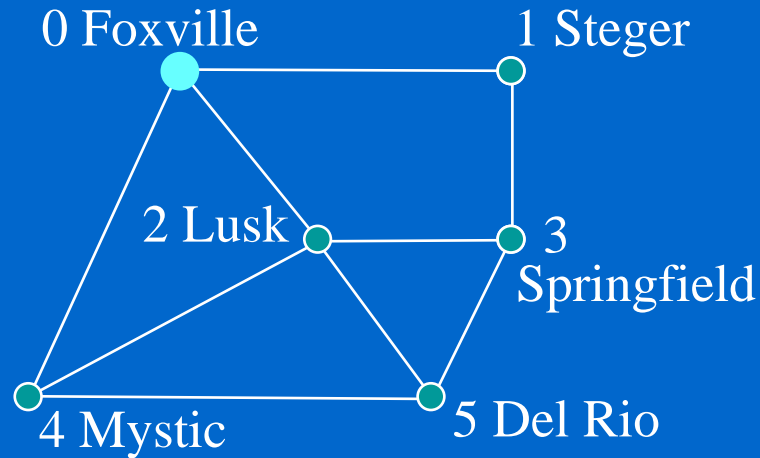


visited

0	1	2	3	4	5
1	1	1	1	0	0

Graph Connectivity - DFS

✧ Depth-First Search

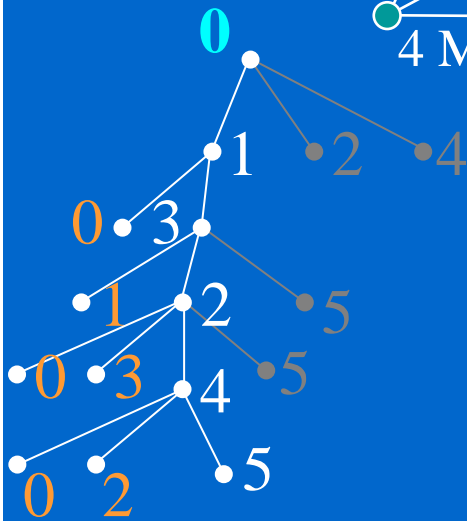
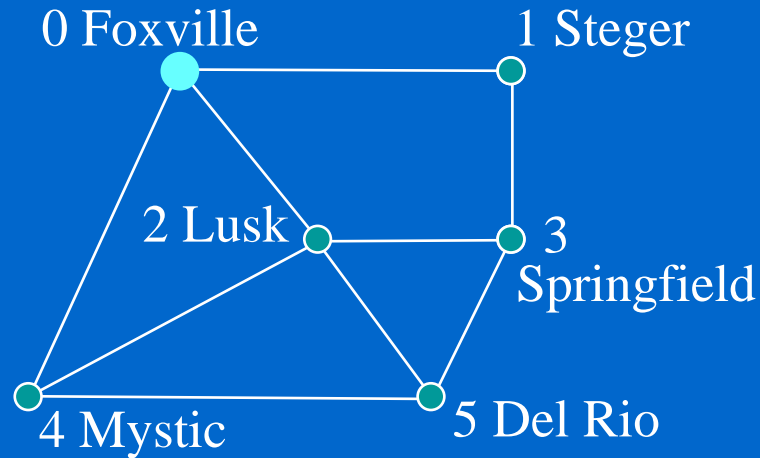


visited

0	1	2	3	4	5
1	1	1	1	1	0

Graph Connectivity - DFS

✧ Depth-First Search

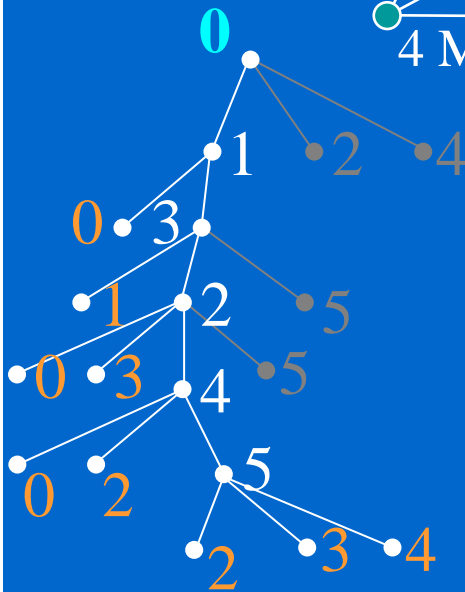
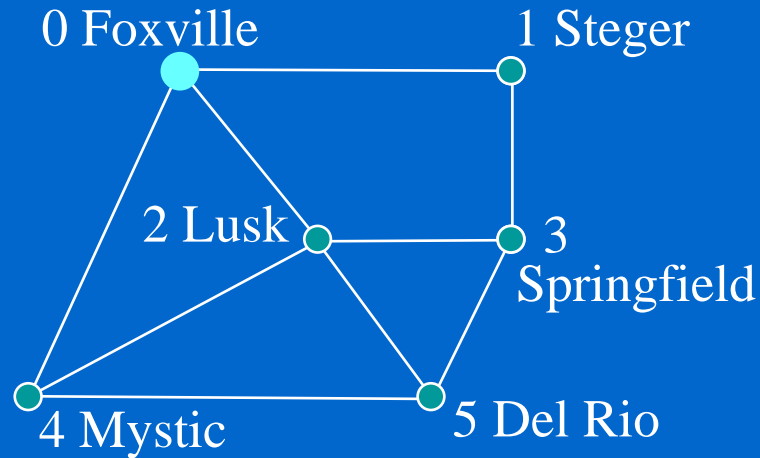


visited

0	1	2	3	4	5
1	1	1	1	1	1

Graph Connectivity - DFS

✧ Depth-First Search

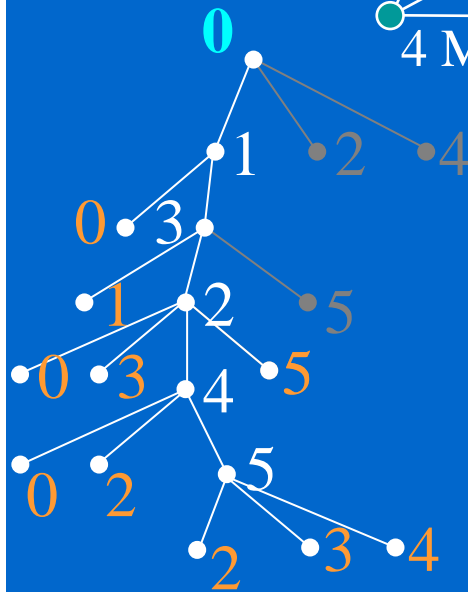
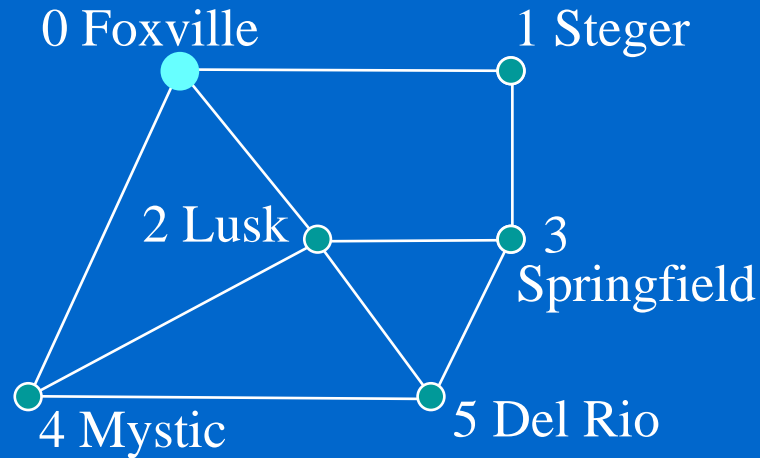


visited

0	1	2	3	4	5
1	1	1	1	1	1

Graph Connectivity - DFS

✧ Depth-First Search

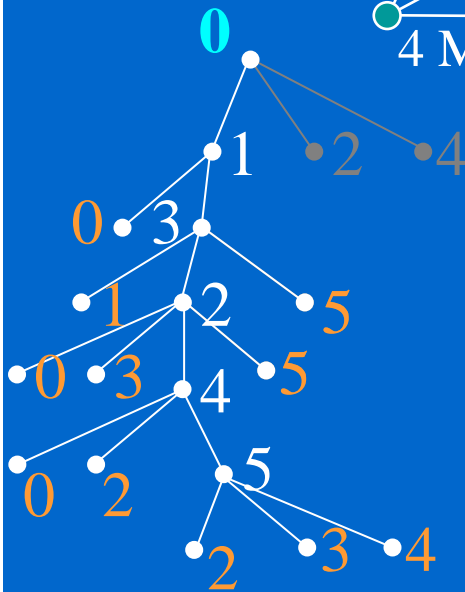
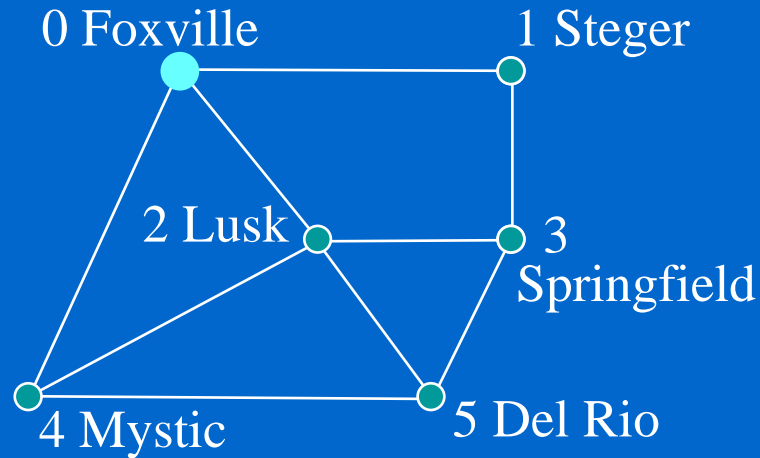


visited

0	1	2	3	4	5
1	1	1	1	1	1

Graph Connectivity - DFS

✧ Depth-First Search

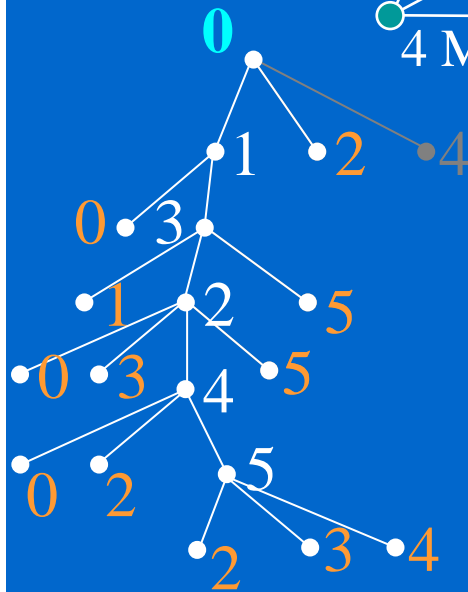
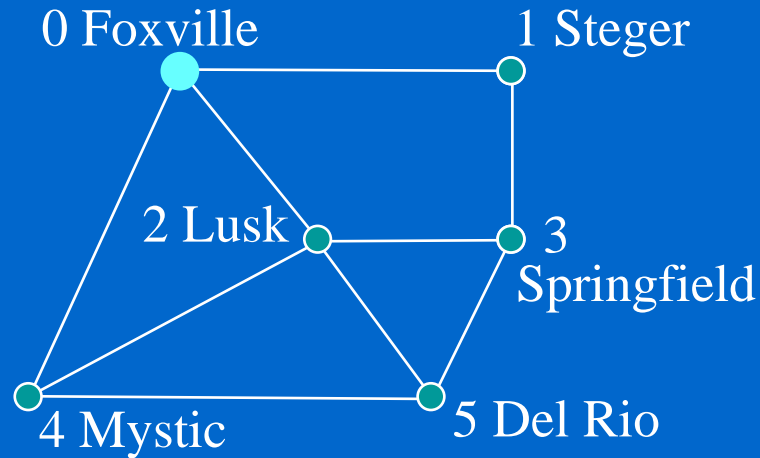


visited

0	1	2	3	4	5
1	1	1	1	1	1

Graph Connectivity - DFS

✧ Depth-First Search

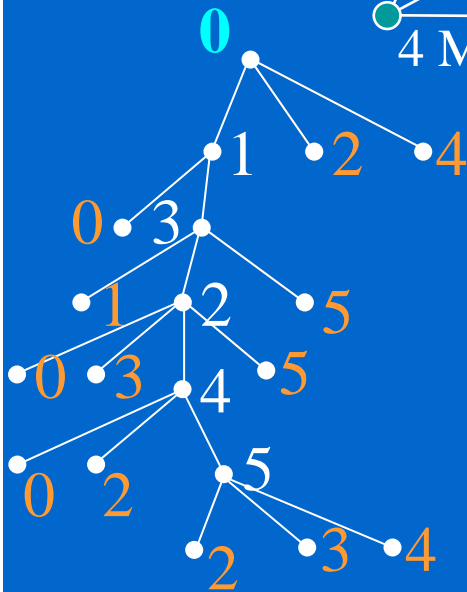
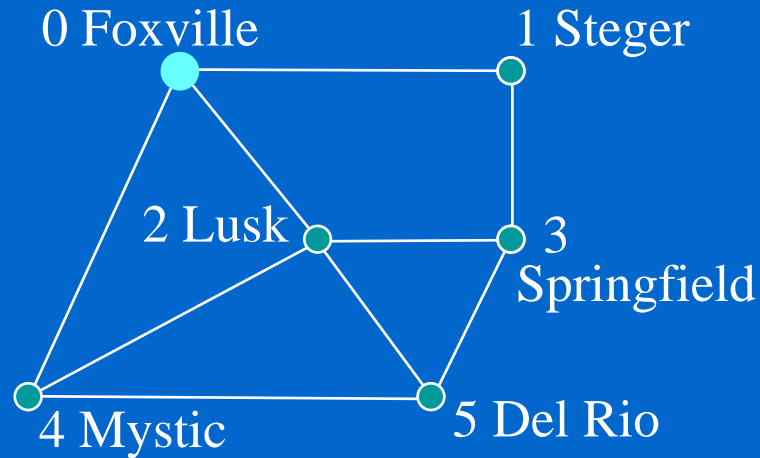


visited

0	1	2	3	4	5
1	1	1	1	1	1

Graph Connectivity - DFS

✧ Depth-First Search

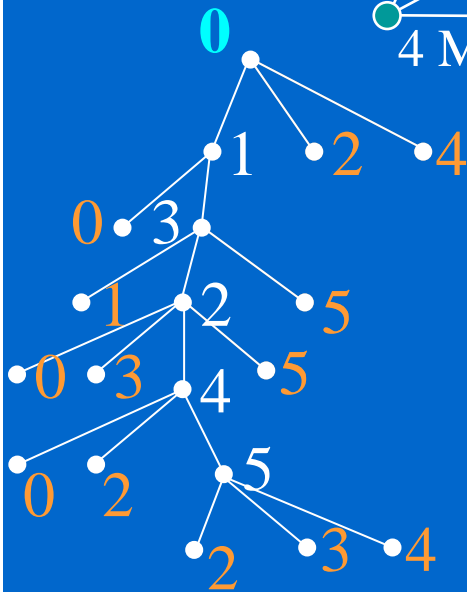
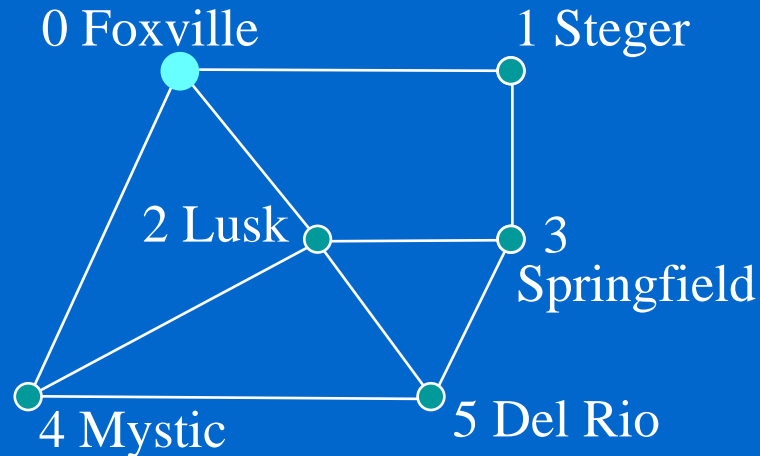


visited

0	1	2	3	4	5
1	1	1	1	1	1

Graph Connectivity - DFS

Depth-First Search



visited

0	1	2	3	4	5
1	1	1	1	1	1

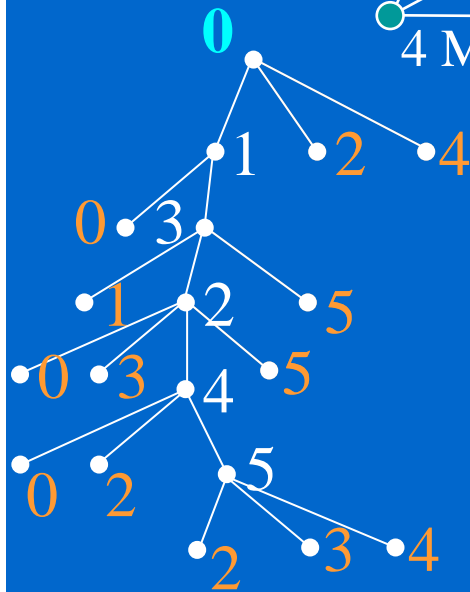
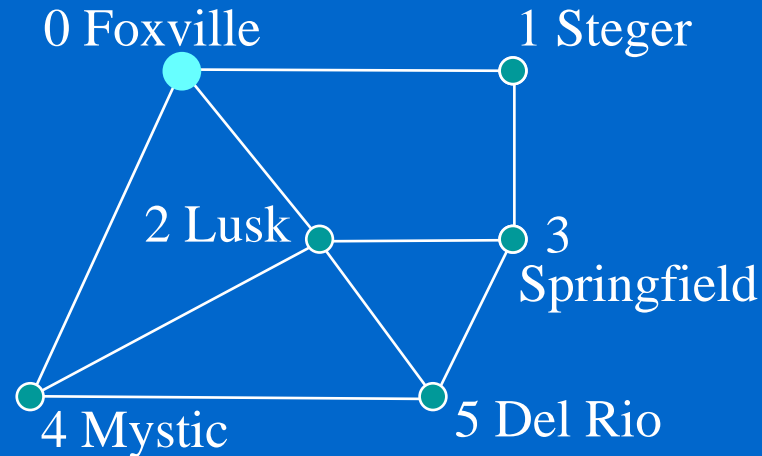
```

vvi W; // global graph
vi visited;

int w[][6] = {{2,4},{3},{0,4,5},
              {1},{0,2,5},{2,4}};
int wn[6] = {2,1,3,1,3,2};
int i, N = 6;
for (i=0; i<N; i++)
    W.pb(vi(w[i],w[i]+wn[i]));
    
```

Graph Connectivity - DFS

Depth-First Search



visited

0	1	2	3	4	5
1	1	1	1	1	1

```
vvi W; // global graph
vi visited;
```

```
int w[][6] = {{2,4},{3},{0,4,5},
              {1},{0,2,5},{2,4}};
```

```
int wn[6] = {2,1,3,1,3,2};
```

```
int i, N = 6;
```

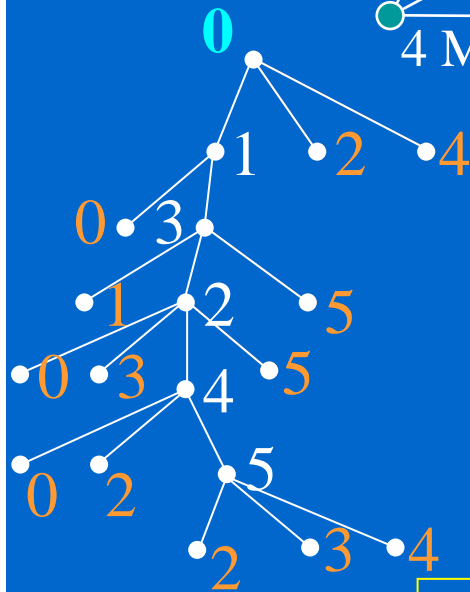
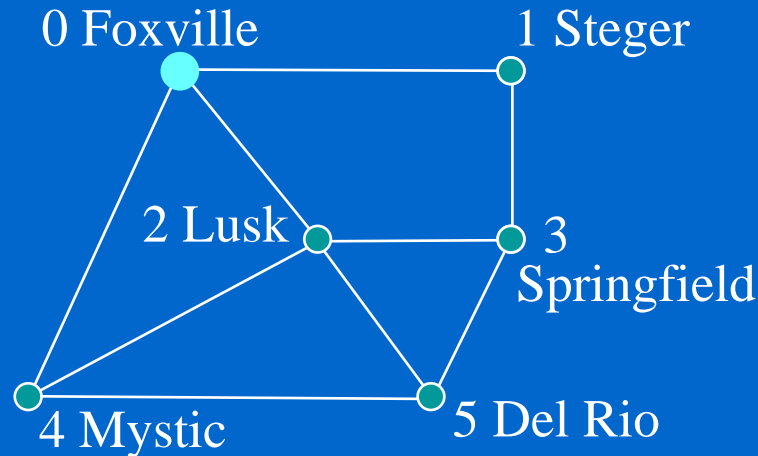
```
for (i=0; i<N; i++)
```

```
W.pb(vi(w[i],w[i]+wn[i]));
```

```
void dfs(int i) {
    if (!visited[i]) {
        visited[i] = 1;
        for_each(all(W[i]), dfs);
    }
}
```

Graph Connectivity - DFS

Depth-First Search



visited

0	1	2	3	4	5
1	1	1	1	1	1

```
vvi W; // global graph
vi visited;

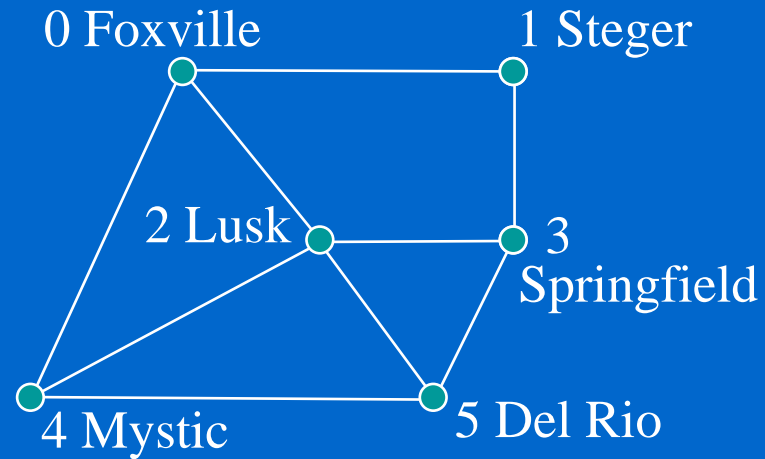
int w[][6] = {{2,4},{3},{0,4,5},
              {1},{0,2,5},{2,4}};
int wn[6] = {2,1,3,1,3,2};
int i, N = 6;
for (i=0; i<N; i++)
    W.pb(vi(w[i],w[i]+wn[i]));
```

```
void dfs(int i) {
    if (!visited[i]) {
        visited[i] = 1;
        for_each(all(W[i]), dfs);
    }
}
```

```
visited = vi(N, 0); dfs(0); // start from vertex 0
if (find(all(visited), 0) == visited.end()) cout << "Connected\n";
```

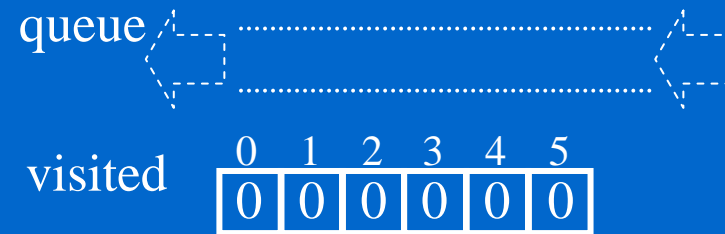
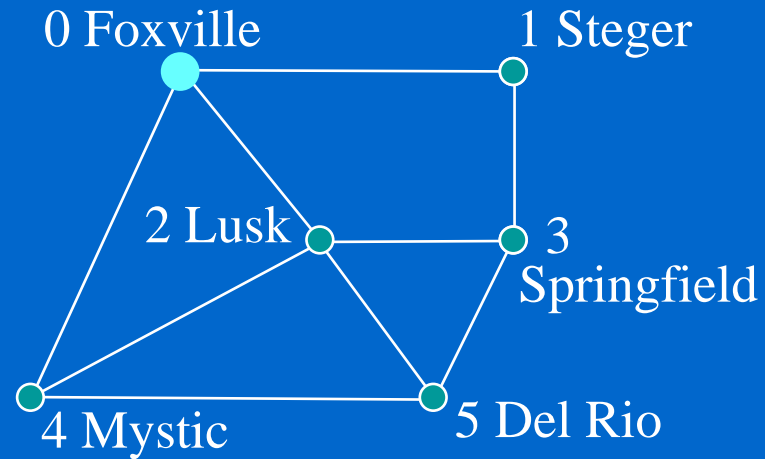
Graph Connectivity - BFS

✧ Breadth-First Search



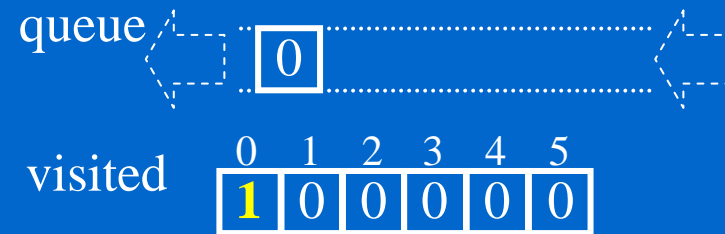
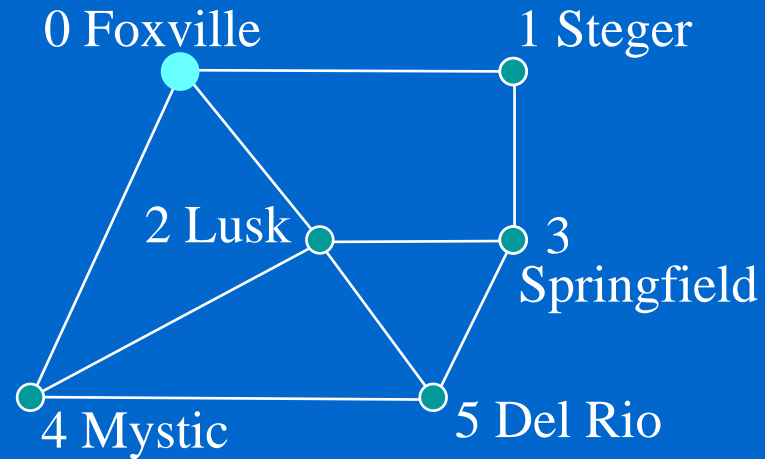
Graph Connectivity - BFS

✧ Breadth-First Search



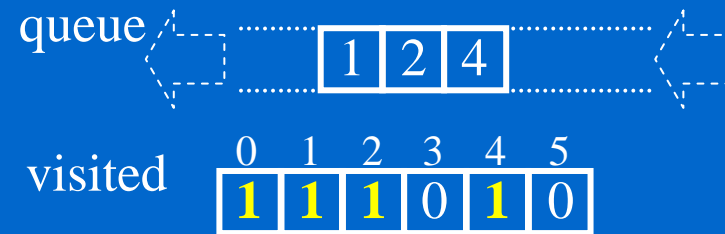
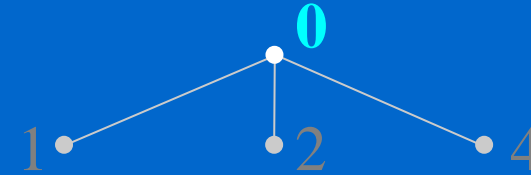
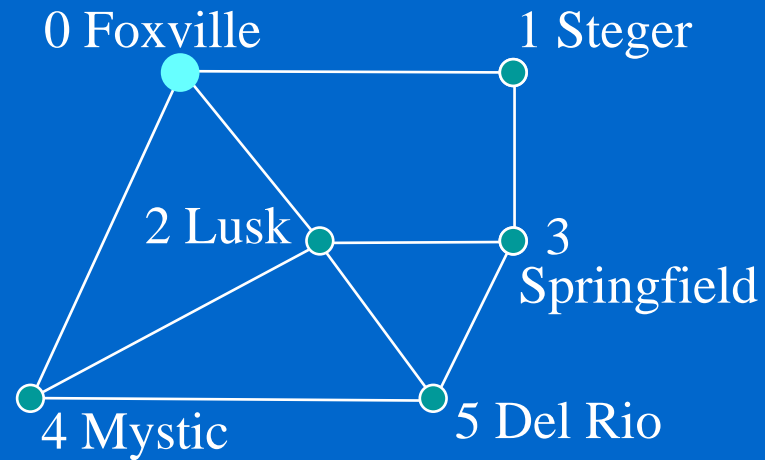
Graph Connectivity - BFS

✧ Breadth-First Search



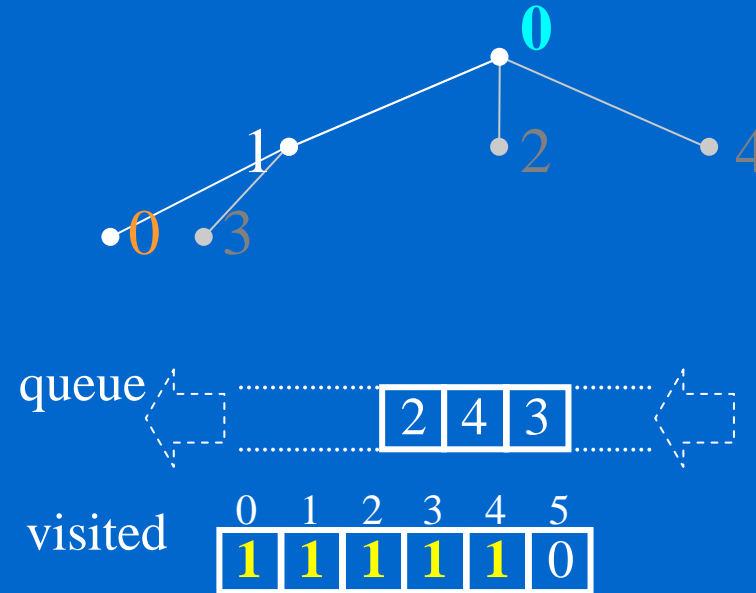
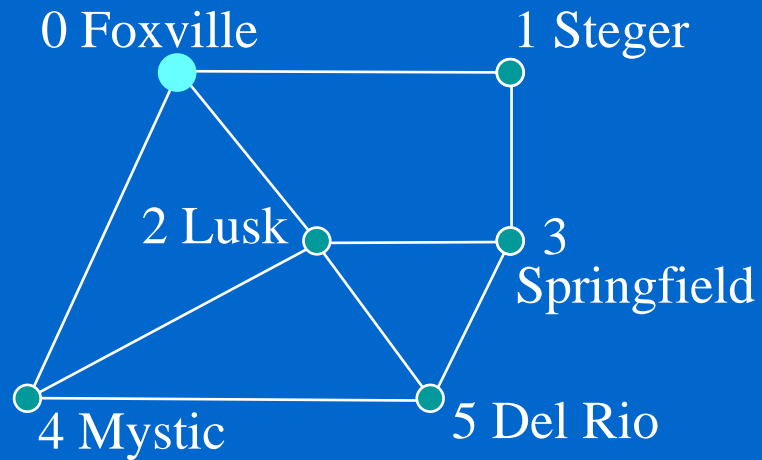
Graph Connectivity - BFS

✧ Breadth-First Search



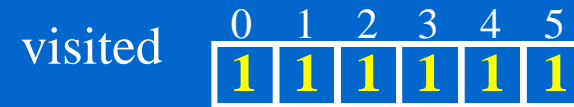
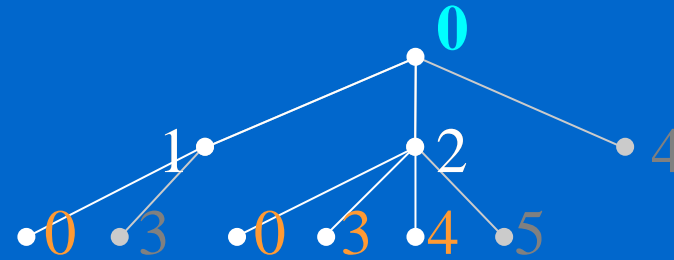
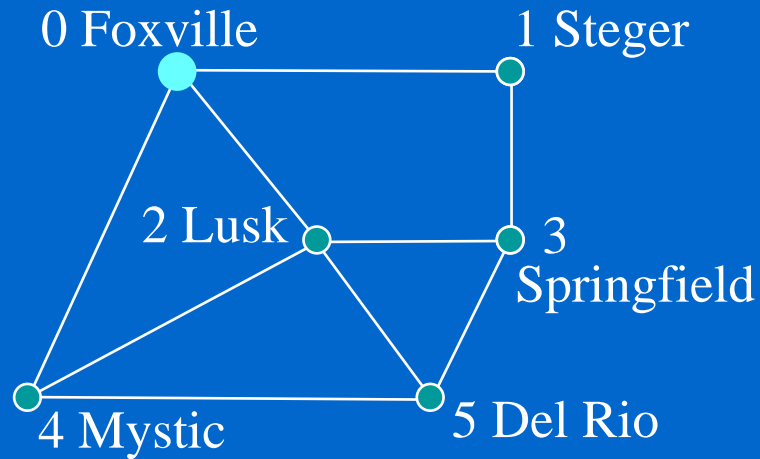
Graph Connectivity - BFS

✧ Breadth-First Search



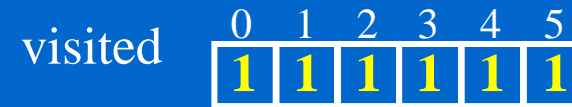
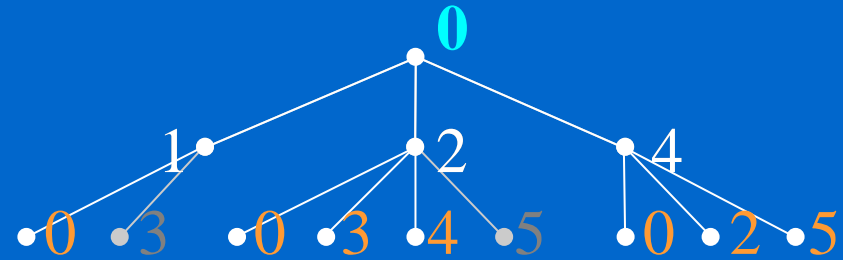
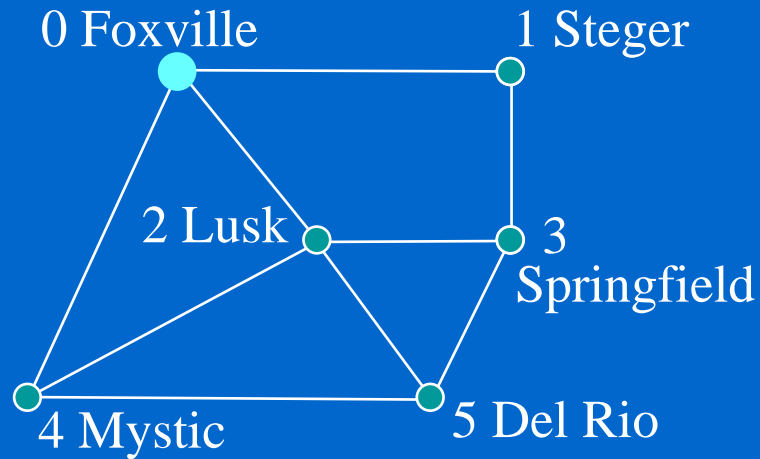
Graph Connectivity - BFS

✧ Breadth-First Search



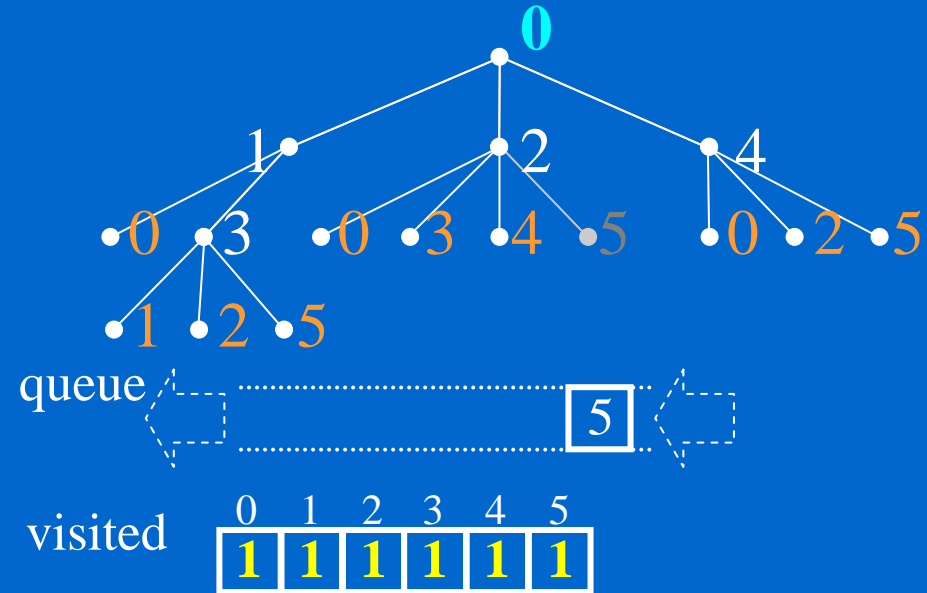
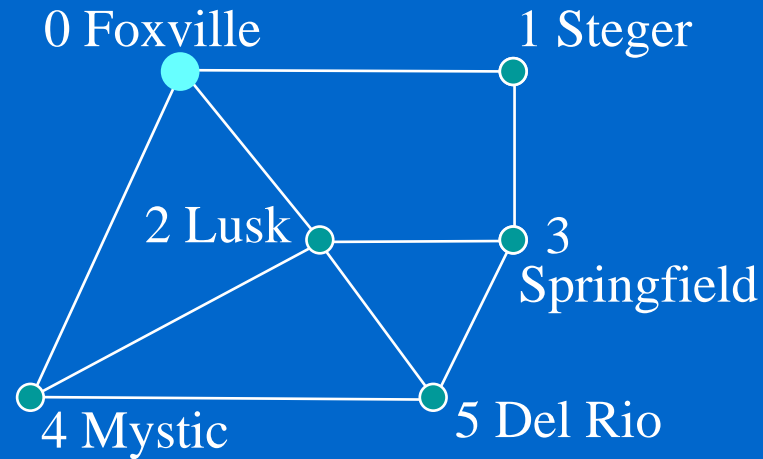
Graph Connectivity - BFS

✧ Breadth-First Search



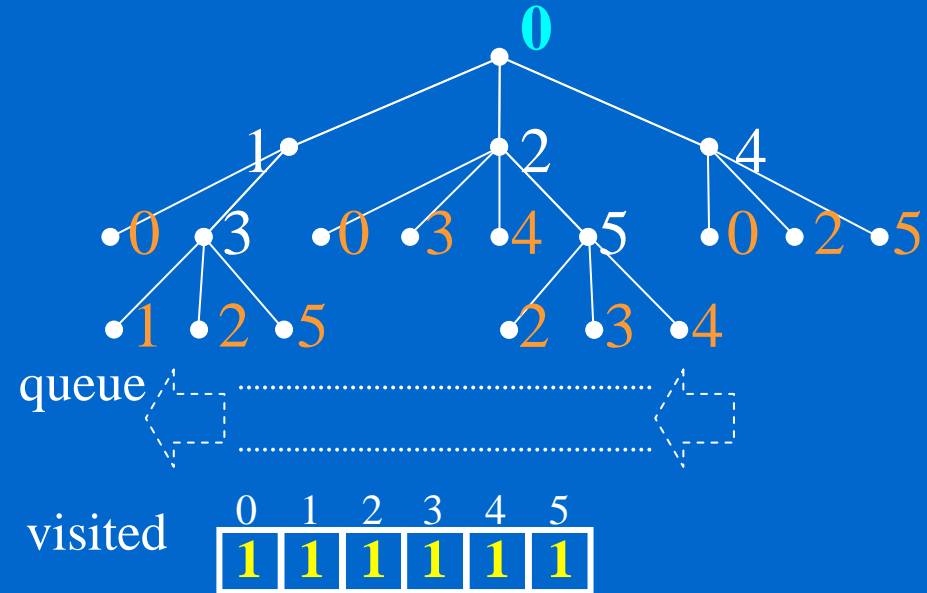
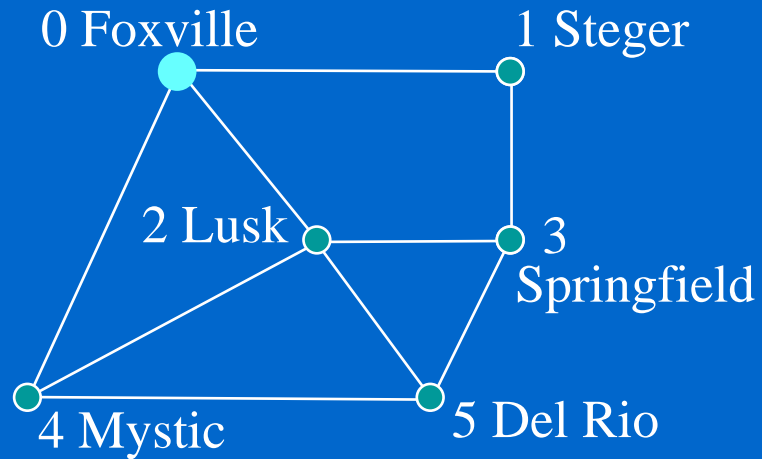
Graph Connectivity - BFS

✧ Breadth-First Search



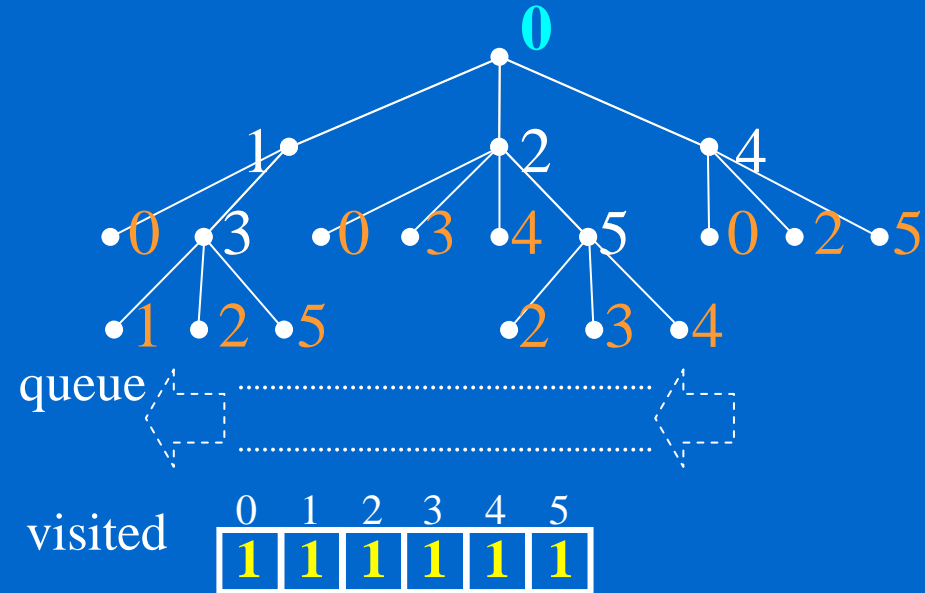
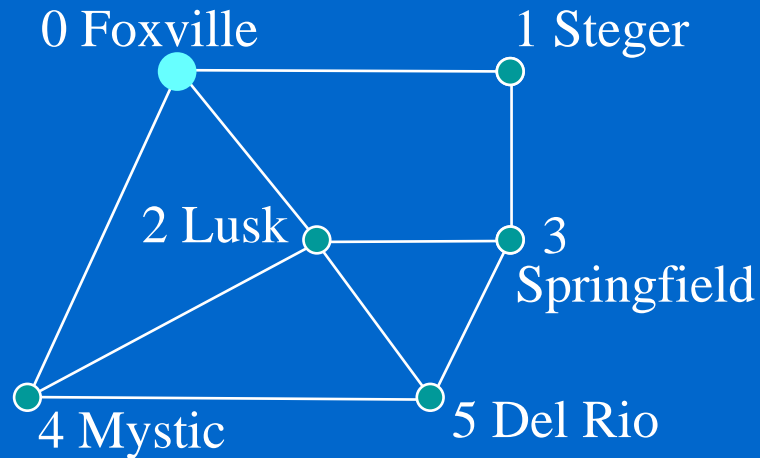
Graph Connectivity - BFS

✧ Breadth-First Search



Graph Connectivity - BFS

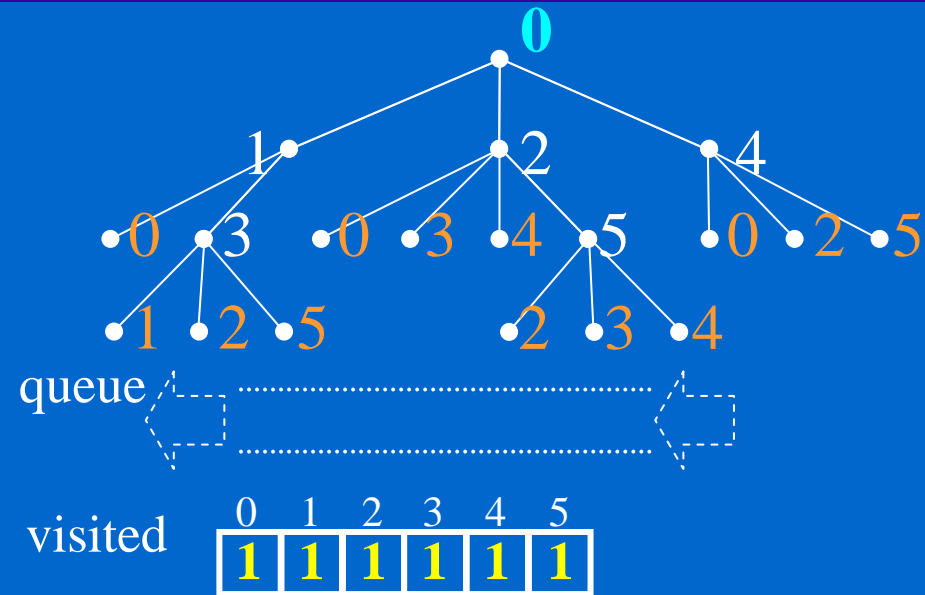
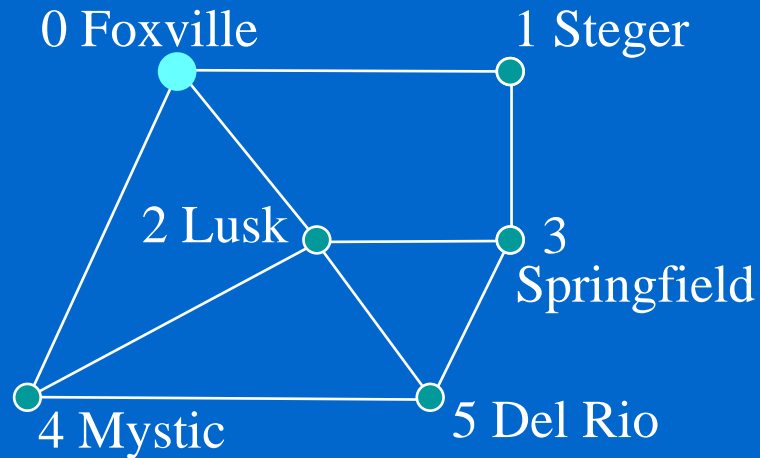
✧ Breadth-First Search



```
vi visited(N, 0);
queue<int> Q;
visited[0] = 1; Q.push(0); // start vertex is 0
while (!Q.empty()) {
    i = Q.front(); Q.pop();
    for (vi::iterator it=W[i].begin(); it!=W[i].end(); ++it)
        if (!visited[*it]) visited[*it] = 1, Q.push(*it);
}
if (find(all(visited), 0) == visited.end()) cout << "Connected\n";
```

Graph Connectivity - BFS

✧ Breadth-First Search



```

vi visited(N, 0);
queue<int> Q;
visited[0] = 1; Q.push(0); // start vertex is 0
while (!Q.empty()) {
    i = Q.front(); Q.pop();
    for (vi::iterator it=W[i].begin(); it!=W[i].end(); ++it)
        if (!visited[*it]) visited[*it] = 1, Q.push(*it);
}
if (find(all(visited), 0) == visited.end()) cout << "Connected\n";
    
```

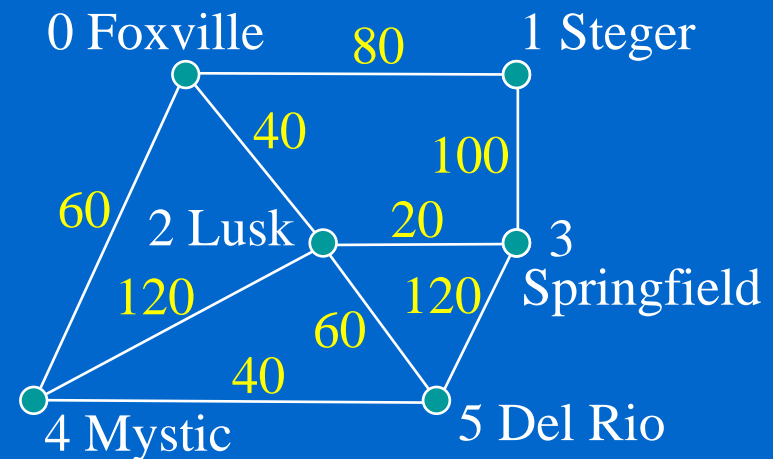
tr (W[i], it) // only for g++

Dijkstra's Shortest Path

```
int i, j, N = 6, w[][6][2] =  
  {{{1,80},{2,40},{4,60}},  
   {{0,80},{3,100}},  
   {{0,40},{3,20},{4,120},{5,60}},  
   {{1,100},{2,20},{5,120}},  
   {{0,60},{2,120},{5,40}},  
   {{2,60},{3,120},{4,40}}};
```

```
int wn[6] = {3,2,4,3,3,3};  
vvi G; // weighted graph  
vii tmp;
```

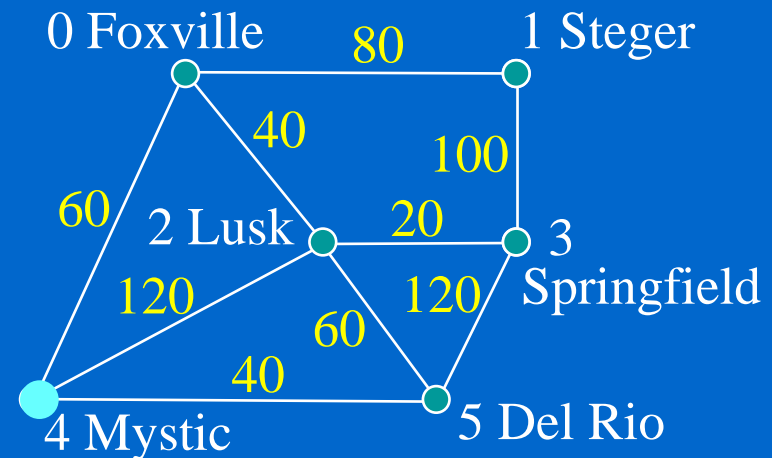
```
for (i=0; i<N; i++) {  
  for (j=0; j<wn[i]; j++)  
    tmp.push_back(pair<int,int>(w[i][j][0],w[i][j][1]));  
  G.push_back(tmp);  
}
```



Dijkstra's Shortest Path (cont'd)

- ❖ implementation with a **priority_queue**

```
vi D(N, 0x7fffffff); // distance from start vertex to each vertex at the moment  
priority_queue<ii,vector<ii>,greater<ii> > Q; // min heap
```

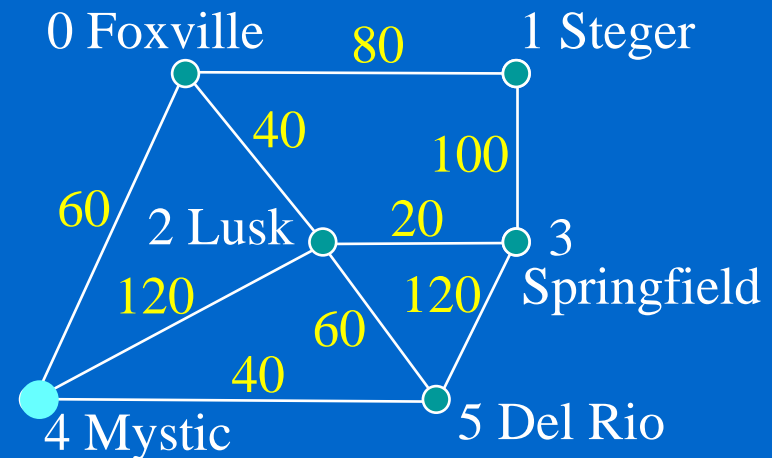


Dijkstra's Shortest Path (cont'd)

- ❖ implementation with a **priority_queue**

```
vi D(N, 0x7fffffff); // distance from start vertex to each vertex at the moment  
priority_queue<ii,vector<ii>,greater<ii> > Q; // min heap
```

```
D[4] = 0; Q.push(ii(D[4],4)); // start vertex: 4
```



Dijkstra's Shortest Path (cont'd)

❖ implementation with a **priority_queue**

```
vi D(N, 0x7fffffff); // distance from start vertex to each vertex at the moment
priority_queue<ii, vector<ii>, greater<ii> > Q; // min heap
```

```
D[4] = 0; Q.push(ii(D[4],4)); // start vertex: 4
```

```
int v, d, v2, cost;
```

```
while (!Q.empty()) {
```

```
    ii top = Q.top(); Q.pop(); // min element
```

```
    v = top.second, d = top.first;
```

```
    if (d <= D[v]) {
```

```
        cout << v << ':' << d << endl;
```

```
        for (vii::iterator it=G[v].begin(); it!=G[v].end(); ++it) {
```

```
            v2 = it->first, cost = it->second;
```

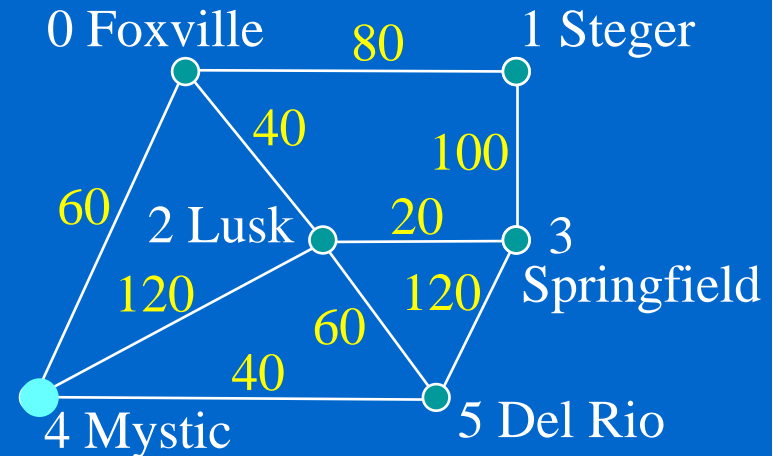
```
            if (d + cost < D[v2])
```

```
                D[v2] = d + cost, Q.push(ii(D[v2], v2));
```

```
        }
```

```
    }
```

```
}
```



Dijkstra's Shortest Path (cont'd)

❖ implementation with a **priority_queue**

```
vi D(N, 0x7fffffff); // distance from start vertex to each vertex at the moment
priority_queue<ii, vector<ii>, greater<ii> > Q; // min heap
```

```
D[4] = 0; Q.push(ii(D[4],4)); // start vertex: 4
```

```
int v, d, v2, cost;
```

```
while (!Q.empty()) {
```

```
    ii top = Q.top(); Q.pop(); // min element
```

```
    v = top.second, d = top.first;
```

```
    if (d <= D[v]) {
```

```
        cout << v << ':' << d << endl;
```

```
        for (vii::iterator it=G[v].begin(); it!=G[v].end(); ++it) {
```

```
            v2 = it->first, cost = it->second;
```

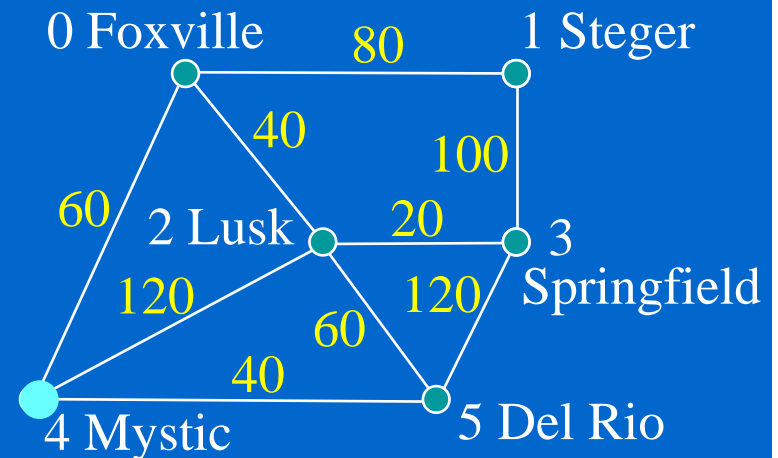
```
            if (d + cost < D[v2])
```

```
                D[v2] = d + cost, Q.push(ii(D[v2], v2));
```

```
        }
```

```
    }
```

```
}
```



there could be multiple entries of the same vertex in the priority queue, only the one that has the least distance ever seen is considered

Dijkstra's Shortest Path (cont'd)

❖ implementation with a **priority_queue**

```
vi D(N, 0x7fffffff); // distance from start vertex to each vertex at the moment
priority_queue<ii, vector<ii>, greater<ii> > Q; // min heap
```

```
D[4] = 0; Q.push(ii(D[4],4)); // start vertex: 4
```

```
int v, d, v2, cost;
```

```
while (!Q.empty()) {
```

```
    ii top = Q.top(); Q.pop(); // min element
```

```
    v = top.second, d = top.first;
```

```
    if (d <= D[v]) {
```

```
        cout << v << ':' << d << endl;
```

```
        for (vii::iterator it=G[v].begin(); it!=G[v].end(); ++it) {
```

```
            v2 = it->first, cost = it->second;
```

```
            if (d + cost < D[v2])
```

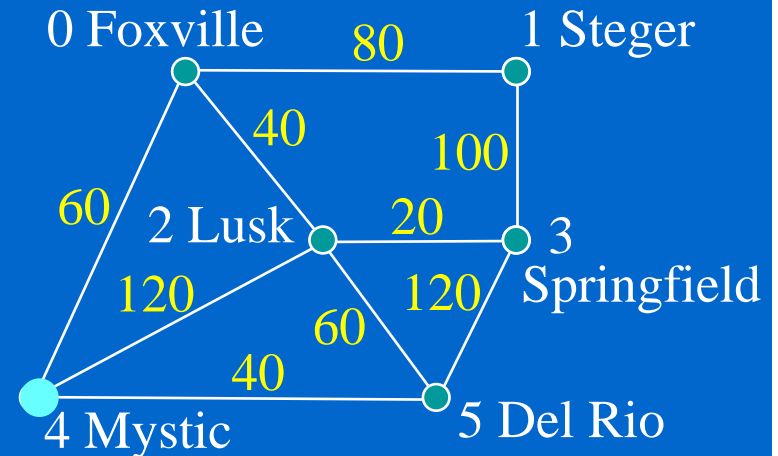
```
                D[v2] = d + cost, Q.push(ii(D[v2], v2));
```

```
        }
```

```
    }
```

```
}
```

there could be multiple entries of the same vertex in the priority queue, only the one that has the least distance ever seen is considered



4:0
5:40
0:60
2:100
3:120
1:140

Dijkstra's Shortest Path (cont'd)

❖ implementation with **set**

```
vi D(N, 0x7fffffff); // distance from start vertex to each vertex at the moment
```

```
set<ii> S; set<ii>::iterator itS;
```

Dijkstra's Shortest Path (cont'd)

❖ implementation with **set**

```
vi D(N, 0x7fffffff); // distance from start vertex to each vertex at the moment
```

```
set<ii> S; set<ii>::iterator itS;
```

```
D[4] = 0; S.insert(ii(D[4],4)); // start vertex: 4
```

Dijkstra's Shortest Path (cont'd)

❖ implementation with **set**

```
vi D(N, 0x7fffffff); // distance from start vertex to each vertex at the moment
```

```
set<ii> S; set<ii>::iterator itS;
```

```
D[4] = 0; S.insert(ii(D[4],4)); // start vertex: 4
```

```
while (!S.empty()) {
```

```
    ii top = *(S.begin()); S.erase(S.begin()); // min element
```

```
    int v = top.second, d = top.first;
```

```
    cout << v << '!' << d << endl;
```

```
    for (vii::iterator it=G[v].begin(); it!=G[v].end(); ++it) {
```

```
        int v2 = it->first, cost = it->second;
```

```
        if (D[v2] > d + cost) { // d==D[v] actually
```

```
            if ((D[v2]!=0x7fffffff)&&(itS=S.find(ii(D[v2],v2)))!=S.end()))
```

```
                S.erase(itS);
```

```
                D[v2] = d + cost; S.insert(ii(D[v2], v2));
```

```
        }
```

```
    }
```

```
}
```


Dijkstra's Shortest Path (cont'd)

❖ implementation with **set**

```
vi D(N, 0x7fffffff); // distance from start vertex to each vertex at the moment
```

```
set<ii> S; set<ii>::iterator itS;
```

```
D[4] = 0; S.insert(ii(D[4],4)); // start vertex: 4
```

```
while (!S.empty()) {
```

```
    ii top = *(S.begin()); S.erase(S.begin()); // min element
```

```
    int v = top.second, d = top.first;
```

```
    cout << v << '!' << d << endl;
```

```
    for (vii::iterator it=G[v].begin(); it!=G[v].end(); ++it) {
```

```
        int v2 = it->first, cost = it->second;
```

```
        if (D[v2] > d + cost) { // d==D[v] actually
```

```
            if ((D[v2]!=0x7fffffff)&&(itS=S.find(ii(D[v2],v2)))!=S.end()))
```

```
                S.erase(itS);
```

```
                D[v2] = d + cost; S.insert(ii(D[v2], v2));
```

```
            }
```

```
        }
```

```
    }
```

 might be erased earlier

Dijkstra's Shortest Path (cont'd)

❖ implementation with **set**

```
vi D(N, 0x7fffffff); // distance from start vertex to each vertex at the moment
```

```
set<ii> S; set<ii>::iterator itS;
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```
D[4] = 0; S.insert(ii(D[4],4)); // start vertex: 4
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while (!S.empty()) {
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    ii top = *(S.begin()); S.erase(S.begin()); // min element
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                S.erase(itS);
```

```
                D[v2] = d + cost; S.insert(ii(D[v2], v2));
```

```
            }
```

```
        }
```

```
    }
```

guarantees no duplicated entry
with the same vertex in the set

might be erased earlier

Dijkstra's Shortest Path (cont'd)

❖ implementation with **set**

```
vi D(N, 0x7fffffff); // distance from start vertex to each vertex at the moment
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set<ii> S; set<ii>::iterator itS;
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D[4] = 0; S.insert(ii(D[4],4)); // start vertex: 4
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```
while (!S.empty()) {
```

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```

```
                S.erase(itS);
```

```
                D[v2] = d + cost; S.insert(ii(D[v2], v2));
```

```
            }
```

```
        }
```

```
    }
```

4:0
5:40
0:60
2:100
3:120
1:140

guarantees no duplicated entry
with the same vertex in the set

might be erased earlier

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